



Integration of Physics-Based and Data-Driven Models for Parameter Estimation: with Applications to Image and Speech Signal Processing

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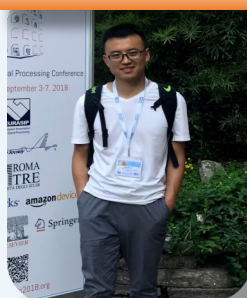
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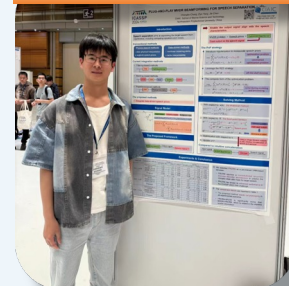
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Parameter Estimation

Scientists and engineers frequently wish to relate physical parameters characterizing a model to collected observations^[1]:

The diagram shows the equation $\mathbf{y} = \mathcal{F}(\mathbf{x}; \mathbf{D}) + \mathbf{n}$ with several annotations. Above the equation, the word "observations" in red has an arrow pointing to $\mathbf{y}$, and the word "parameters" in red has an arrow pointing to $\mathbf{x}$. Below the equation, the words "forward model" in blue have an arrow pointing to $\mathcal{F}$, and the word "noise" in blue has an arrow pointing to $\mathbf{n}$. The variables $\mathbf{y}$, $\mathbf{x}$, and $\mathbf{n}$ are each enclosed in a small red square box, while $\mathcal{F}$ and $\mathbf{D}$ are enclosed in small blue square boxes.

$$\mathbf{y} = \mathcal{F}(\mathbf{x}; \mathbf{D}) + \mathbf{n}$$

Three fundamental problems:

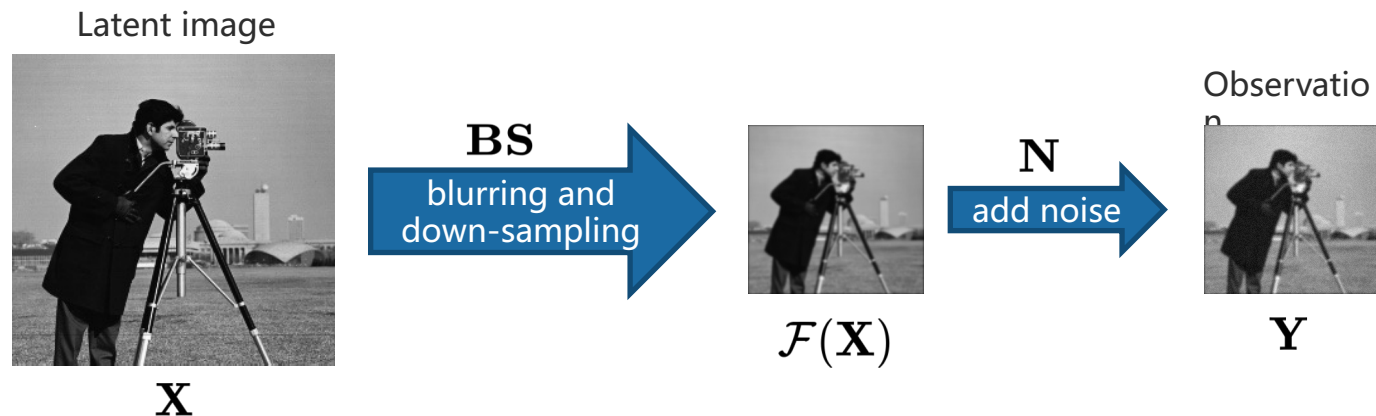
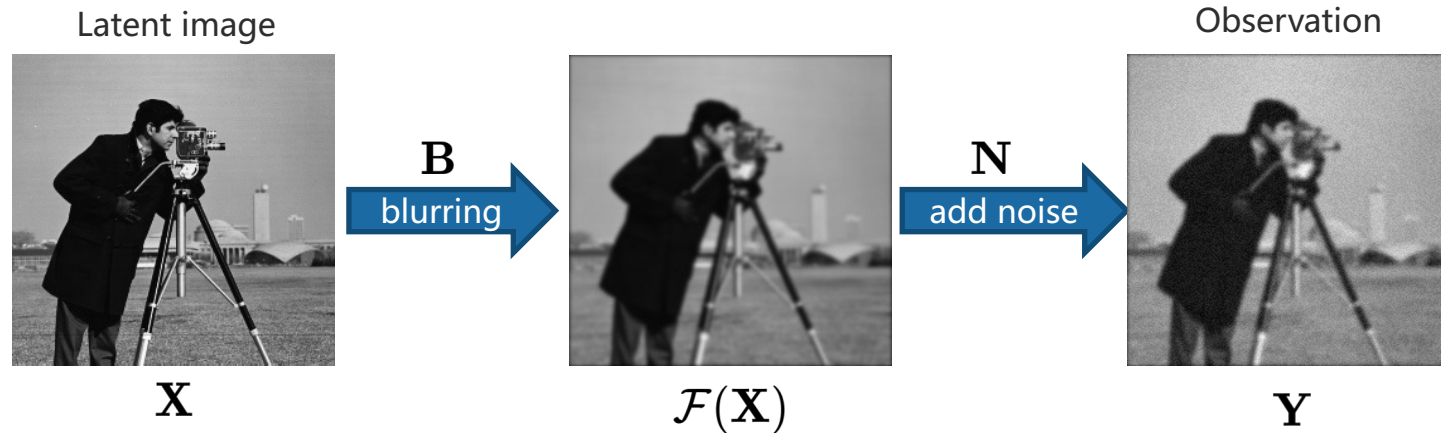
- Forward problem: to find $\mathbf{y}$ given $\mathbf{x}$ (and other information or data $\mathbf{D}$);
- **Parameter estimation (inverse) problem:** to find $\mathbf{x}$ given $\mathbf{y}$ (and $\mathbf{D}$);
- System identification: to determine $\mathcal{F}(\cdot)$ given $\mathbf{x}$ and $\mathbf{y}$ (and $\mathbf{D}$).

[1] R. Aster, B. Borchers, and C. Thurber, "Parameter Estimation and Inverse Problems", Elsevier, 2011.

Parameter Estimation

Example 1 - image processing :

Recover the latent clean image from its degraded observation.

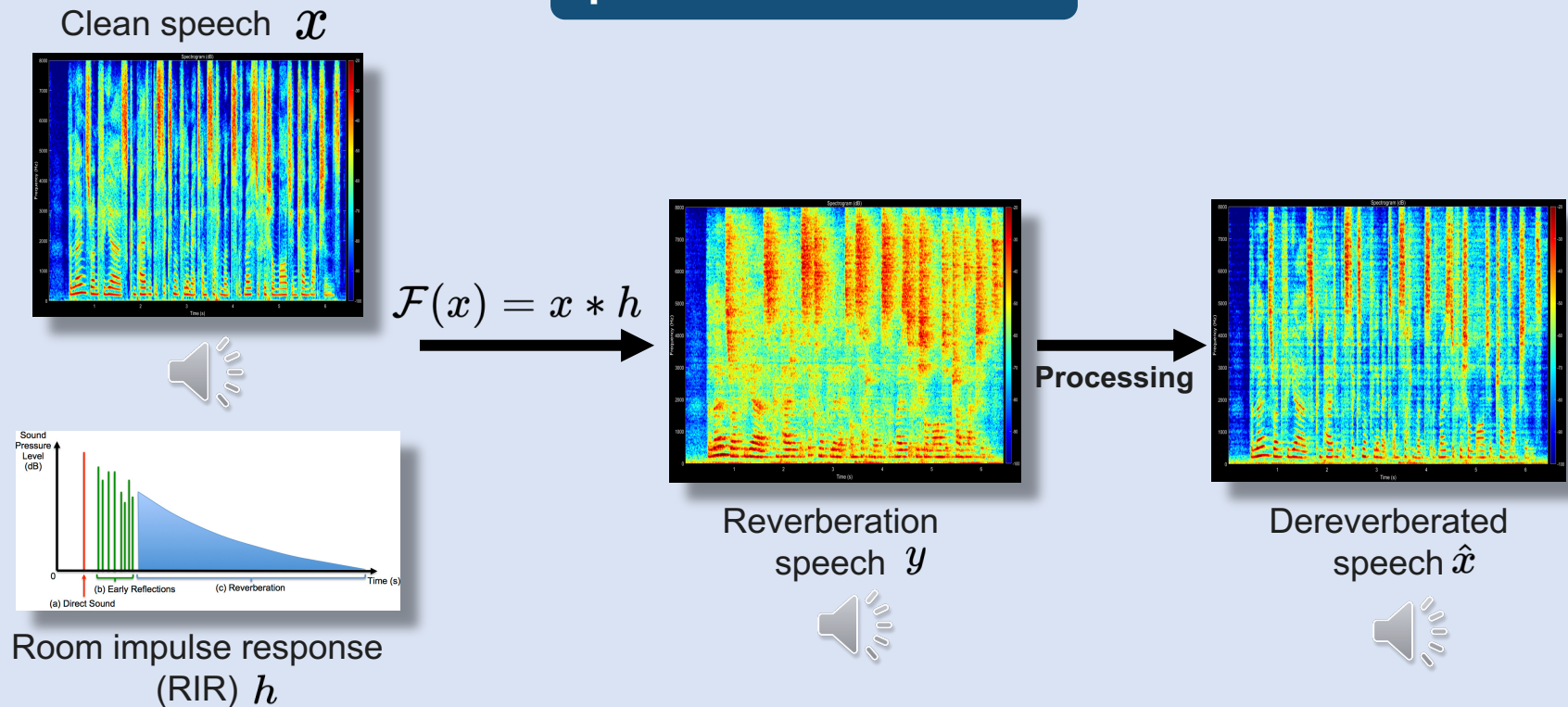


Parameter Estimation

Example 2 – Speech signal processing:

Recover the clean speech from its corrupted observation.

speech dereverberation



Objective: to improve speech clarity and intelligibility

Physics-based Models

Grounded in expert knowledge, solved via numerical methods, e.g.,

- Inverse filtering / deconvolution;
- Beamforming;
- Least square methods;
- Matrix/Tensor factorization.



Pros

Incorporate models based on physical mechanisms



Clear interpretation



Cons

Without fully exploring the inherent data priors



Limited performance

Data-driven Models

Powered by historical data, guided by machine learning, e.g.,

- Kernel machine;
- Manifold learning;
- Deep neural networks;



Pros

Rapidly developed deep neural networks in particular



Powerful capability



Cons

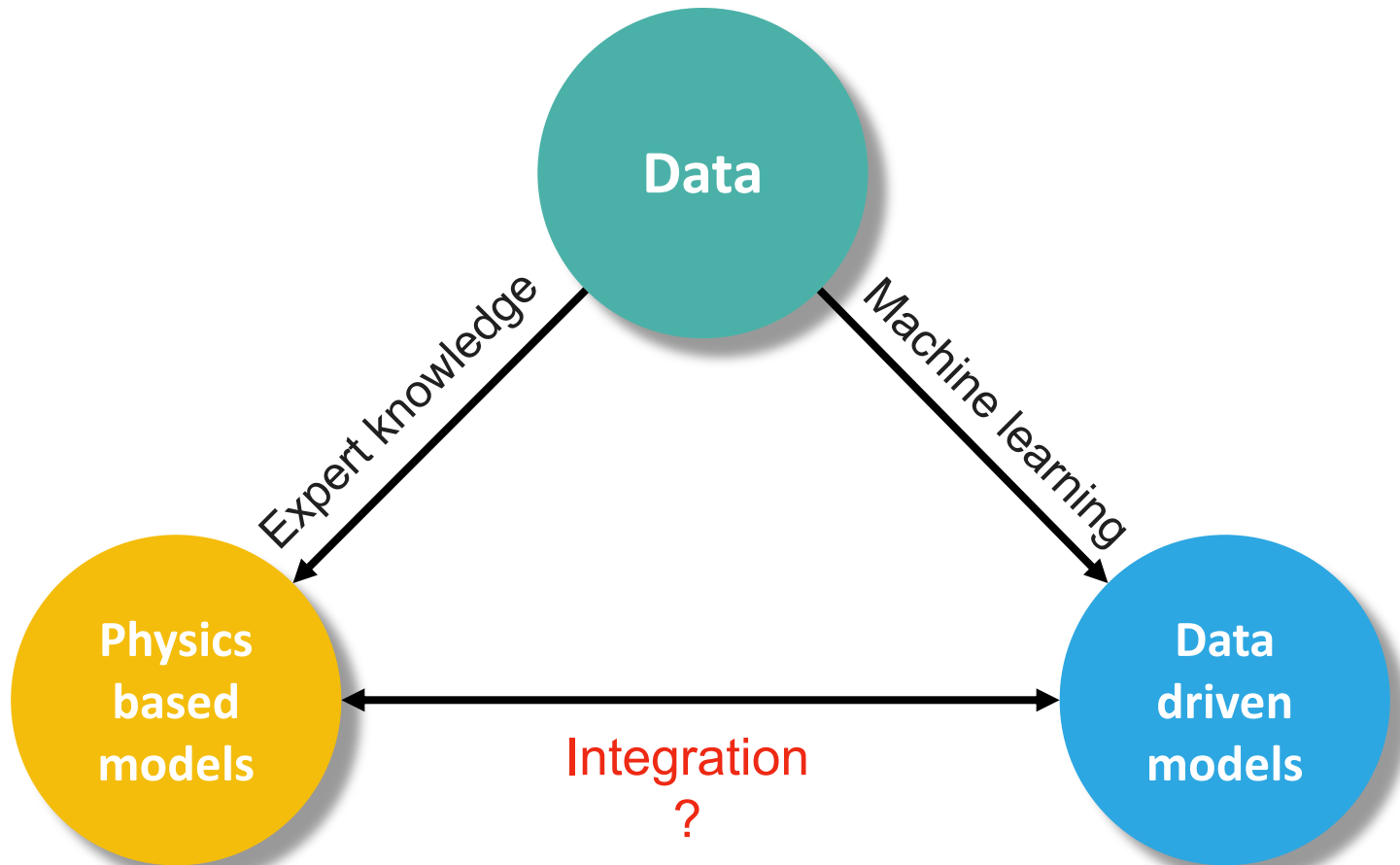
Directly applying can be black boxes



Less interpretable or general

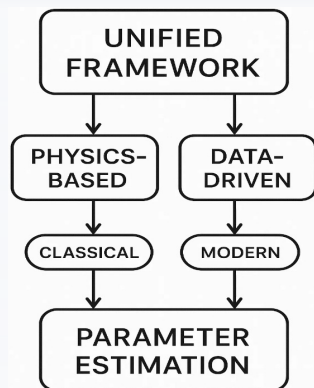
Motivations

? Is it possible to leverage the advantages of both physics-based and data-driven models?



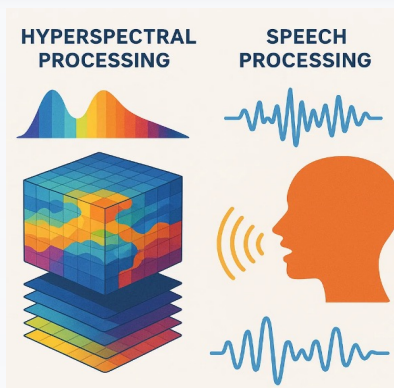
Takeaways from this Tutorial

1. Unified Framework



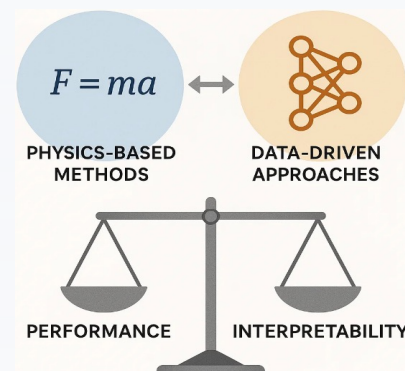
- A unified framework with **hybrid strategy** that accommodates both classical and modern parameter estimation methods

2. Cross-domain Applicability



- The hybrid methodology can be extended to a **wide range** of signal processing applications, such as image processing and speech processing

3. Bridging Interpretability & Performance



- Physics-based methods provide **interpretability**, while data-driven approaches offer **flexibility**.

➤ This tutorial is based upon (but not limited to) our papers:

[1] J. Chen, M. Zhao, X. Wang, C. Richard and S. Rahardja, “Integration of physics-based and data-driven models for hyperspectral image unmixing: A summary of current methods”. In: IEEE Signal Processing Magazine 40.2 (2023), pp. 61–74.

[2] Z. Yang, W. Yang, K. Xie and J. Chen, “Integrating Data Priors with Weighted Prediction Error for Speech Dereverberation”, IEEE/ACM Transactions on Audio, Speech, Language and Processing, vol. 32, pp. 3908-3923, 2024.

Outline

Introduction

Part I: Methodology

- General Problem Formulation

- Hybrid Approaches for Parameter Estimation

- State-of-the-Art Hybrid Techniques

Part II: Applications to Image Processing

- Background in Hyperspectral Imaging

- Hybrid Strategies for Hyperspectral Deconvolution

- Hybrid Strategies for Hyperspectral Fusion

- Hybrid Strategies for Hyperspectral Unmixing

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General Problem Formulation

A general parameter estimation problem:

$$\text{find } \mathbf{x} \quad s.t. \quad \mathbf{y} = \mathcal{F}(\mathbf{x}) + \mathbf{n}.$$

Maximum A Posteriori (MAP) formulation:

$$\begin{aligned} \hat{\mathbf{x}} &= \arg \max_{\mathbf{x}} \{ \log p(\mathbf{y}|\mathbf{x}) \log p(\mathbf{x}) \} \\ &= \arg \min_{\mathbf{x}} \left\{ \frac{1}{2\sigma^2} \|\mathbf{y} - \mathcal{F}(\mathbf{x})\|^2 + \alpha \mathcal{R}(\mathbf{x}) \right\}. \end{aligned}$$


i.i.d. Gaussian

Regularized optimization:

$$\begin{aligned} \hat{\mathbf{x}} &= \arg \min_{\mathbf{x}} \{ \mathcal{L}(\hat{\mathbf{y}}, \mathbf{y}) + \lambda \mathcal{R}(\mathbf{x}) \} \\ &= \arg \min_{\mathbf{x}} \left\{ \|\mathbf{y} - \mathcal{F}(\mathbf{x})\|^2 + \lambda \mathcal{R}(\mathbf{x}) \right\} \quad \text{with } \hat{\mathbf{y}} = \mathcal{F}(\mathbf{x}). \end{aligned}$$

This problem can have different problem formulations depending on whether $\mathcal{F}(\cdot)$ is (partially) known or not^[1].

[1] J. Chen, M. Zhao, X. Wang, C. Richard and S. Rahardja, "Integration of physics-based and data-driven models for hyperspectral image unmixing: A summary of current methods". In: IEEE Signal Processing Magazine 40.2 (2023), pp. 61–74.

General Problem Formulation

Problem formulation 1: Assuming $\mathcal{F}(\cdot)$ is known, the formulation is

$$\hat{\mathbf{x}} = \underset{\mathbf{x}}{\arg \min} \{ \mathcal{L}(\hat{\mathbf{y}}, \mathbf{y}) + \lambda \mathcal{R}(\mathbf{x}) \}$$

with $\hat{\mathbf{y}} = \mathcal{F}(\mathbf{x})$.

Examples:

- Least square methods^[1]:

$$\hat{\mathbf{x}} = \arg \min_{\mathbf{x}} \{ \|\mathbf{y} - \mathbf{A}\mathbf{x}\|^2 + \lambda \mathcal{R}(\mathbf{x}) \}.$$

- Regularized nonnegative matrix factorization^[2]

$$\hat{\mathbf{X}} = \arg \min_{\mathbf{X}} \{ \|\mathbf{Y} - \mathbf{A}\mathbf{X}\|_{\text{F}}^2 + \lambda \mathcal{R}(\mathbf{A}, \mathbf{X}) \}.$$

[1] D. Heinz and C. Chang, "Fully constrained least squares linear spectral mixture analysis method for material quantification in hyperspectral imagery". In: IEEE Trans. Geosci. Remote Sens. 39.3 (2001), 529–545.

[2] J. Peng, W. Sun, H. Li, W. Li, X. Meng, C. Ge, and Q. Du, "Low-rank and sparse representation for hyperspectral image processing: A review". In: IEEE Geosci. Remote Sens. Mag. 10.1 (2021), 10–43.

General Problem Formulation

Problem formulation 2: Assuming $\mathcal{F}(\cdot)$ is (partially) unknown, the formulation is

$$\hat{\mathbf{x}} = \underset{\mathbf{x}, \mathcal{F}}{\arg \min} \{ \mathcal{L}(\hat{\mathbf{y}}, \mathbf{y}) + \lambda \mathcal{R}(\mathbf{x}) \}$$

with $\hat{\mathbf{y}} = \mathcal{F}(\mathbf{x})$.

Examples:

- Kernel-based learning approaches^[1]

$$\{\hat{\mathbf{x}}, \hat{\mathcal{F}}\} = \arg \min_{\mathbf{x}, \mathcal{F} \in \mathcal{H}_{\text{RKHS}}} \{ \|\mathbf{y} - \mathcal{F}(\mathbf{x})\|^2 + \lambda \mathcal{R}(\mathcal{F}, \mathbf{x}) \}.$$

- Manifold learning methods^[2]

$$\mathbf{y} = \mathcal{C}(\mathbf{A}\mathbf{x}) + \mathbf{n}.$$

[1] J. Chen, C. Richard, and P. Honeine, "Nonlinear estimation of material abundances in hyperspectral images with l1-norm spatial regularization," IEEE Trans. Geosci. Remote Sens., vol. 52, no. 5, pp. 2654–2665, 2013.

[2] R. Heylen, M. Parente, and P. Gader, "A review of nonlinear hyperspectral unmixing methods," IEEE J. Sel. Top. Appl. Earth Observat. Remote Sens., vol. 7, no. 6, pp. 1844–1868, 2014.

General Problem Formulation

Problem formulation 3: Assuming $\mathcal{F}(\cdot)$ is (partially) unknown, the optimization formulation jointly

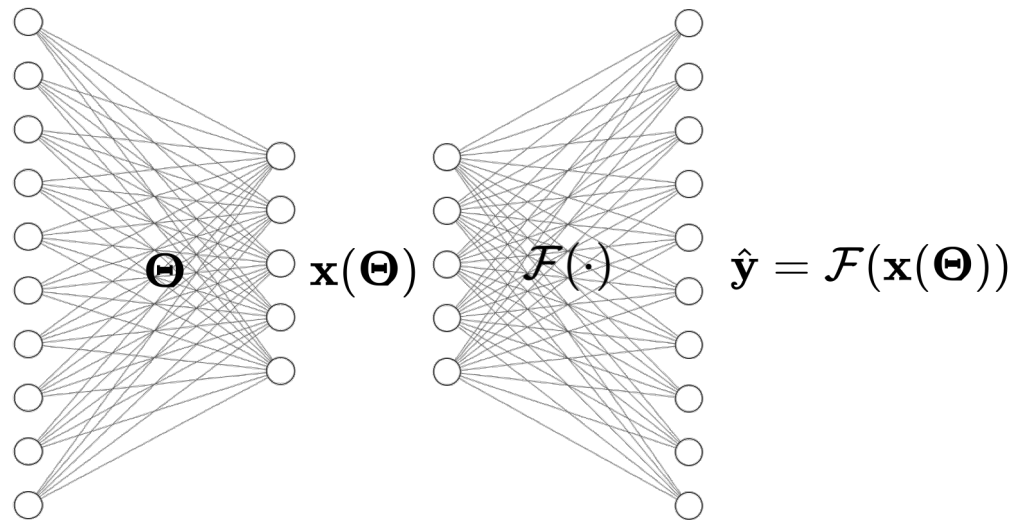
- Learn $\mathcal{F}(\cdot)$ from data;
- Considers re-parameterizing $\mathbf{x}$.

$$\{\hat{\mathbf{x}}, \Theta^*\} = \arg \min_{\mathbf{x}, \Theta, \mathcal{F}} \{ \mathcal{L}(\hat{\mathbf{y}}, \mathbf{y}) + \lambda \mathcal{R}(\mathbf{x}) \}$$

with $\hat{\mathbf{y}} = \mathcal{F}(\mathbf{x}(\Theta))$.

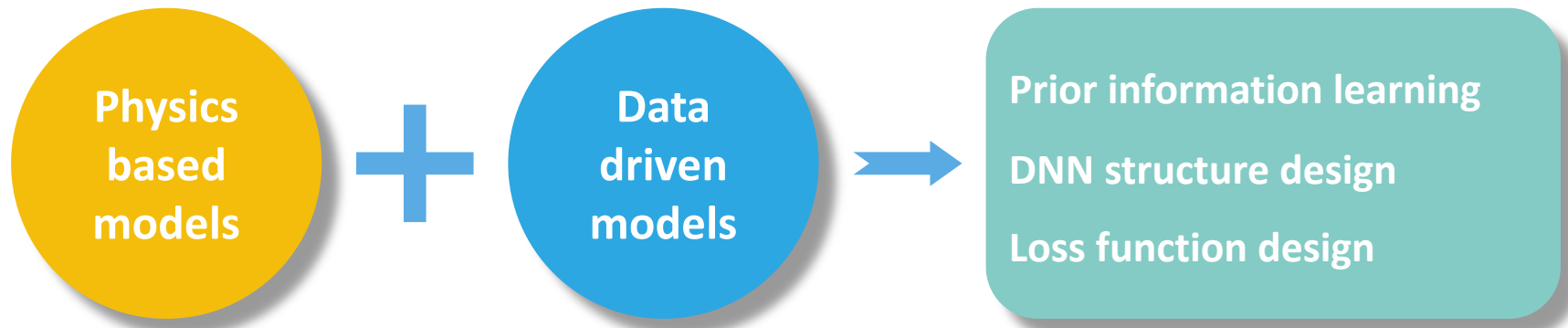
— design of $\mathcal{R}$?

Examples:



Hybrid Approaches for Parameter Estimation

Recent physics-based data-driven methods show their power in improving the following three aspects^{[1][2]}:



[1] J. Chen, M. Zhao, X. Wang, C. Richard and S. Rahardja, "Integration of physics-based and data-driven models for hyperspectral image unmixing: A summary of current methods". In: IEEE Signal Processing Magazine 40.2 (2023), pp. 61–74.

[2] G. E. Karniadakis, I. G. Kevrekidis, L. Lu, P. Perdikaris, S. Wang, and L. Yang, "Physics-informed machine learning," Nature Reviews Physics, vol. 3, no. 6, pp. 422–440, 2021.

Prior Information Learning - I

Problem formulation 1:

$$\hat{\mathbf{x}} = \underset{\mathbf{x}}{\arg \min} \{ \mathcal{L}(\hat{\mathbf{y}}, \mathbf{y}) + \lambda \mathcal{R}(\mathbf{x}) \}$$

with $\hat{\mathbf{y}} = \mathcal{F}(\mathbf{x})$.

Deep prior regularization^[1]: plug the output of a DNN into the objective function by defining

$$\begin{aligned} \mathcal{R}(\mathbf{x}) &= d(\mathbf{x}, \tilde{\mathbf{x}})^2, \\ \text{s.t. } \tilde{\mathbf{x}} &= \text{DNN}(\mathbf{y}). \end{aligned}$$

Examples:

- The Frobenius norm^[1]: $\mathcal{R}(\mathbf{x}) = \|\mathbf{x} - \tilde{\mathbf{x}}\|^2$;
- The 2D Total Variation (TV) norm^[2]: $\mathcal{R}(\mathbf{x}) = \|\mathbf{x} - \tilde{\mathbf{x}}\|_{TV} + \|\mathbf{x}\|_{TV}$.

[1] X. Wang, J. Chen, Q. Wei, and C. Richard, "Hyperspectral image superresolution via deep prior regularization with parameter estimation," IEEE Trans. Circuits Syst. Video Technol., 2021.

[2] M. Vella, B. Zhang, W. Chen, and J. F. C. Mota, "Enhanced hyperspectral image super-resolution via rgb fusion and tv-tv minimization," in Proc. IEEE Int. Conf. Image Process. (ICIP), 2021.

Prior Information Learning - II

Problem formulation 1:

$$\hat{\mathbf{x}} = \underset{\mathbf{x}}{\arg \min} \{ \mathcal{L}(\hat{\mathbf{y}}, \mathbf{y}) + \lambda \mathcal{R}(\mathbf{x}) \}$$

with $\hat{\mathbf{y}} = \mathcal{F}(\mathbf{x})$.

Plug-and-play framework^[1]: Plug the denoiser into optimization, without need to explicitly define $\mathcal{R}(\mathbf{x})$.

$$\begin{aligned}\mathbf{x}^{(k+1)} &= \arg \min_{\mathbf{x}} \mathcal{L}(\mathcal{F}(\mathbf{x}), \mathbf{y}) + \frac{\rho}{2} \|\mathbf{x} - \mathbf{z}^{(k)} + \mathbf{v}^{(k)}\|_2^2 \\ \mathbf{z}^{(k+1)} &= \frac{\rho}{2} \|\mathbf{x} - \mathbf{z}^{(k)} + \mathbf{v}^{(k)}\|_2^2 + \lambda \mathcal{R}(\mathbf{x}) = \text{Denoiser}(\mathbf{x}^{(k+1)} + \mathbf{v}^{(k)}) \\ \mathbf{v}^{(k+1)} &= \mathbf{v}^{(k)} + \mathbf{x}^{(k+1)} - \mathbf{z}^{(k+1)}\end{aligned}$$

Examples:

- Plug-and-play ADMM^[1];
- Regularization by Denoising (RED)^[2].

[1] S. V. Venkatakrishnan, C. A. Bouman, and B. Wohlberg, "Plug-and-play priors for model-based reconstruction," in Proc. IEEE Global Conf. Signal Inf. Process. (GlobalSIP), Austin, TX, USA, pp. 945–948, Dec. 2013.

[2] Y. Romano, M. Elad, and P. Milanfar, "The little engine that could: Regularization by denoising (RED)," SIAM J. Imaging Sci., vol. 10, no. 4, pp. 1804–1844, 2017.

Prior Information Learning - III

Problem formulation 1:

$$\hat{\mathbf{x}} = \underset{\mathbf{x}}{\arg \min} \{ \mathcal{L}(\hat{\mathbf{y}}, \mathbf{y}) + \lambda \mathcal{R}(\mathbf{x}) \}$$

with $\hat{\mathbf{y}} = \mathcal{F}(\mathbf{x})$.

Deep unrolling framework **unfolds iterative optimization** into a trainable **end-to-end deep network**.

The sparse coding problem:

$$\hat{\mathbf{x}} = \arg \min_{\mathbf{x}} \left\{ \frac{1}{2} \|\mathbf{Ax} - \mathbf{y}\|^2 + \lambda \|\mathbf{x}\|_1 \right\}.$$

Iterative Optimization

$$\mathbf{x}^{(k+1)} = \eta_{\lambda\alpha} \left(\mathbf{x}^{(k)} - \alpha \mathbf{A}^\top (\mathbf{Ax}^{(k)} - \mathbf{y}) \right).$$

Unrolled Deep Network

$$\mathbf{x}^{(k+1)} = \eta_{\theta^{(k)}} \left(\mathbf{W}_1 \mathbf{y} + \mathbf{W}_2 \mathbf{x}^{(k)} \right).$$



Examples:

- Learned ISTA^[1]
- ADMM-net^[2]

[1] K. Gregor and Y. LeCun, "Learning fast approximations of sparse coding," in Proc. 27th Int. Conf. Mach. Learn. (ICML), 2010, pp. 399–406.

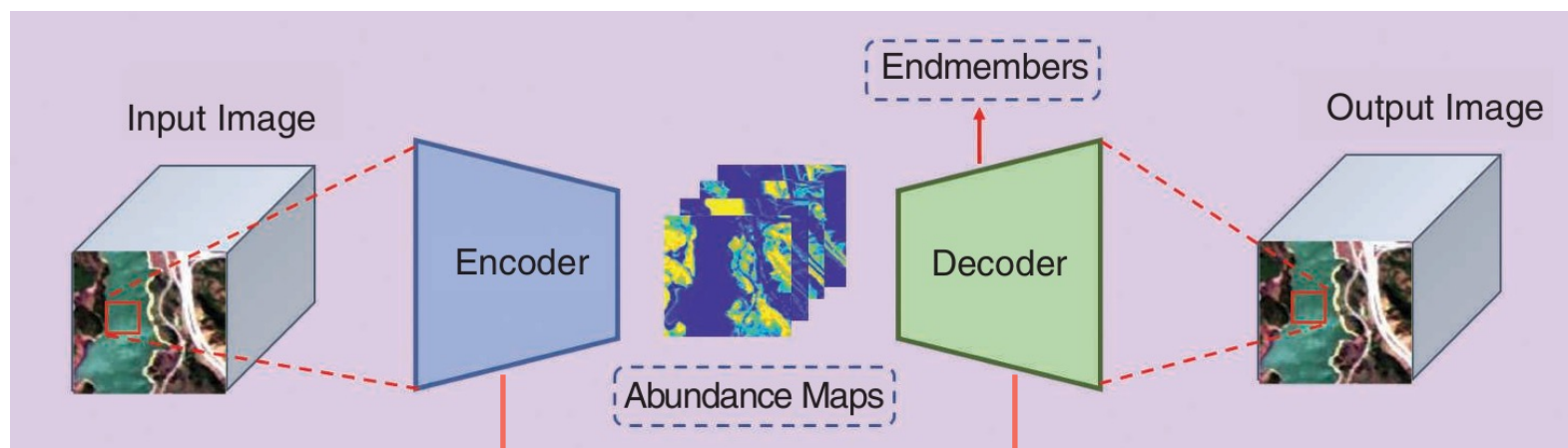
[2] Y. Yang, J. Sun, H. Li, and Z. Xu, "Deep ADMM-Net for compressive sensing MRI," in Adv. Neural Inf. Process. Syst. (NeurIPS), 2016, pp. 10–18.

DNN structure design

Problem formulation 3:

$$\{\hat{\mathbf{x}}, \Theta^*\} = \arg \min_{\mathbf{x}, \Theta, \mathcal{F}} \{\mathcal{L}(\hat{\mathbf{y}}, \mathbf{y}) + \lambda \mathcal{R}(\mathbf{x})\}$$

with $\hat{\mathbf{y}} = \mathcal{F}(\mathbf{x}(\Theta)).$



Encoder Design $\mathcal{Q} = f_{\Theta_{\text{enc}}}(y)$

- **FCN / CNN / Multistream encoders**
- **Kernel-based encoders** (Riemannian metric, spectral correlation)
- **Variational encoders (VAE)** for probabilistic modeling
- **Multibranch / multitask encoders** to capture spectral-spatial priors

$\hat{y} = f_{\Theta_{\text{dec}}}(\mathcal{Q})$ Decoder Design

- **Linear decoder** $\hat{y} = W\Theta$
- **Postnonlinear decoder** $\hat{y} = \Psi(W\Theta)$
- **Additive nonlinear decoder** $\hat{y} = W\Theta + \Psi(W\Theta)$
- **Bilinear decoder** $\hat{y} = W\Theta + Db$
- **Endmember-generating decoder**
 $\hat{y} = f_{\Theta_{\text{end}}}(z) = \Psi(z)$

Loss function design

Problem formulation 3:

$$\{\hat{\mathbf{x}}, \Theta^*\} = \arg \min_{\mathbf{x}, \Theta, \mathcal{F}} \{\mathcal{L}(\hat{\mathbf{y}}, \mathbf{y}) + \lambda \mathcal{R}(\mathbf{x})\}$$

with $\hat{\mathbf{y}} = \mathcal{F}(\mathbf{x}(\Theta))$.

Physically inspired cost functions have been proposed recently to enhance performance.

Examples:

1. General geometric distances:

- Mean-squared error (MSE)^[1] $\mathcal{L}_{\text{MSE}} = \frac{1}{N} \sum_{i=1}^N \|y_i - \hat{y}_i\|^2$ -----> Sensitive to the scale of spectra
 - Spectral angle distance (SAD) $\mathcal{L}_{\text{SAD}} = \frac{1}{N} \sum_{i=1}^N \arccos\left(\frac{\langle y_i, \hat{y}_i \rangle}{\|y_i\| \|\hat{y}_i\|}\right)$
 - Spectral information divergence (SID) $\mathcal{L}_{\text{SID}} = \frac{1}{N} \sum_{i=1}^N p_i \log\left(\frac{p_i}{\hat{p}_i}\right)$
- } Scale invariant

[1] S. Ozkan, B. Kaya, and G. B. Akar, "EndNet: Sparse autoencoder network for endmember extraction and hyperspectral unmixing," IEEE Trans. Geosci. Remote Sens., vol. 57, no. 1, pp. 482–496, Jan. 2019.

Loss function design

Problem formulation 3:

$$\{\hat{\mathbf{x}}, \Theta^*\} = \arg \min_{\mathbf{x}, \Theta, \mathcal{F}} \{\mathcal{L}(\hat{\mathbf{y}}, \mathbf{y}) + \lambda \mathcal{R}(\mathbf{x})\}$$

with $\hat{\mathbf{y}} = \mathcal{F}(\mathbf{x}(\Theta))$.

Physically inspired cost functions have been proposed recently to enhance performance.

Examples:

2. Deep learning metrics:

- Generative adversarial networks (GANs)^[1] $\mathcal{L}_{\mathcal{G}} = \mathcal{L}_{\text{AE}} + \mathcal{L}_{\text{adv}}$
 - The perceptual loss^[2] $\mathcal{L}_{\text{Perceptual}} = \frac{1}{N} \sum_{i=1}^N \|\mathcal{P}(y_i) - \mathcal{P}(\hat{y}_i)\|^2$
- Discriminator: distinguish between the real and generated samples
- a feature extractor
- Generator: Generate samples that are similar to real data

[1] Q. Jin, Y. Ma, F. Fan, J. Huang, X. Mei, and J. Ma, "Adversarial autoencoder network for hyperspectral unmixing," IEEE Trans. Neural Netw. Learn. Syst., early access, 2022.

[2] L. Gao, Z. Han, D. Hong, B. Zhang, and J. Chanussot, "CyCU-Net: Cycle consistency unmixing network by learning cascaded autoencoders," IEEE Trans. Geosci. Remote Sens., vol. 60, 2022.

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Part III: Applications to Speech Signal Processing

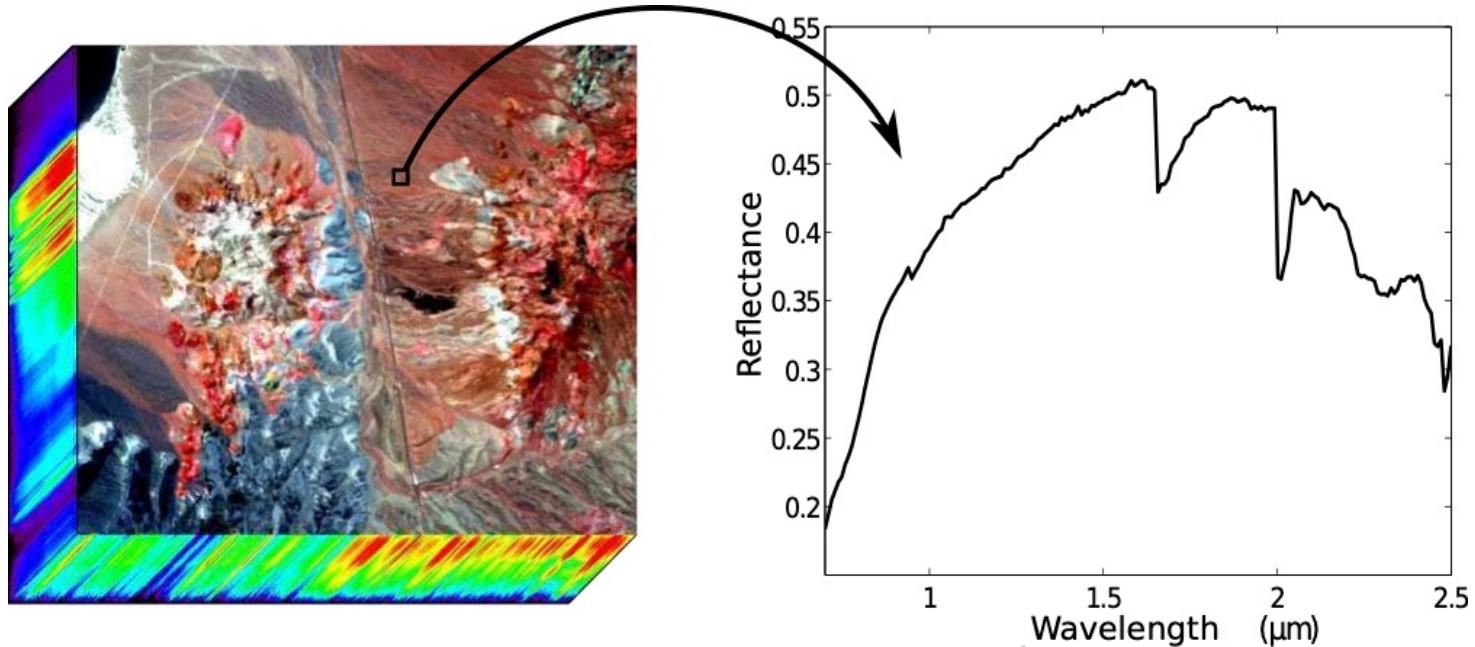
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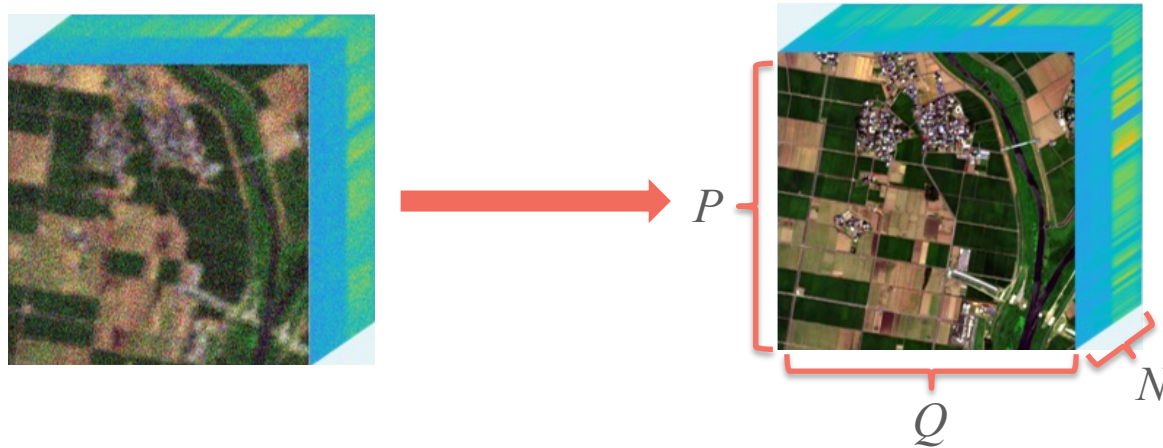
Future Directions

Background in Hyperpsectral Imaging



- High spectral resolution (hundreds of spectral bands);
- Core part of many applications, e.g., remote sensing, medical imaging, etc.

Background in Hyperspectral Imaging



An illustration of hyperspectral deconvolution

The abundant spectral information makes hyperspectral image processing more complex than ordinary 2D images:

- Spatial prior;
- Spectral prior.

Hybrid Strategies for Hyperspectral Deconvolution

Problem formulation 1:

$$\hat{\mathbf{x}} = \underset{\mathbf{x}}{\arg \min} \{ \mathcal{L}(\hat{\mathbf{y}}, \mathbf{y}) + \lambda \mathcal{R}(\mathbf{x}) \}$$

with $\hat{\mathbf{y}} = \mathcal{F}(\mathbf{x})$.

Linear degradation model:

$$\mathbf{Y}_i = \mathcal{H}_i * \mathbf{X}_i + \mathbf{N}_i, \quad \forall i.$$

This model can be written as^[1]:

$$\mathbf{y} = \mathbf{H}\mathbf{x} + \mathbf{n},$$



The optimization problem:

$$\hat{\mathbf{x}} = \arg \min_{\mathbf{x}} \left\{ \frac{1}{2} \|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2 + \lambda \mathcal{R}(\mathbf{x}) \right\}.$$

The prior information of $\mathbf{x}$ is encoded in $\mathcal{R}(\mathbf{x})$.

[1] X. Wang, J. Chen, and C. Richard, "Tuning-free plug-and-play hyperspectral image deconvolution with deep priors," IEEE Transactions on Geoscience and Remote Sensing, vol. 61, pp. 1–13, 2023.

Hybrid Strategies for Hyperspectral Deconvolution

Constrained optimization:

$$\hat{\mathbf{x}} = \arg \min_{\mathbf{x}} \frac{1}{2} \|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2 + \lambda \mathcal{R}(\mathbf{z}), \quad \text{s. t.} \quad \mathbf{z} = \mathbf{x}.$$

Augmented Lagrangian :

$$\mathcal{L}_{\rho}(\mathbf{x}, \mathbf{z}, \mathbf{v}) = \arg \min_{\mathbf{x}} \frac{1}{2} \|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2 + \lambda \Phi(\mathbf{z}) + \mathbf{v}^T (\mathbf{x} - \mathbf{z}) + \frac{\rho}{2} \|\mathbf{x} - \mathbf{z}\|^2.$$

Variable splitting based on ADMM:

$$\begin{aligned} \mathbf{x}_{k+1} &= \arg \min_{\mathbf{x}} \frac{1}{2} \|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2 + \frac{\rho_k}{2} \|\mathbf{x} - \tilde{\mathbf{x}}_k\|^2 \\ \mathbf{z}_{k+1} &= \arg \min_{\mathbf{z}} \lambda \Phi(\mathbf{z}) + \frac{\rho_k}{2} \|\tilde{\mathbf{z}}_k - \mathbf{z}\|^2 \\ \mathbf{u}_{k+1} &= \mathbf{u}_k + \mathbf{x}_{k+1} - \mathbf{z}_{k+1} \end{aligned}$$

where

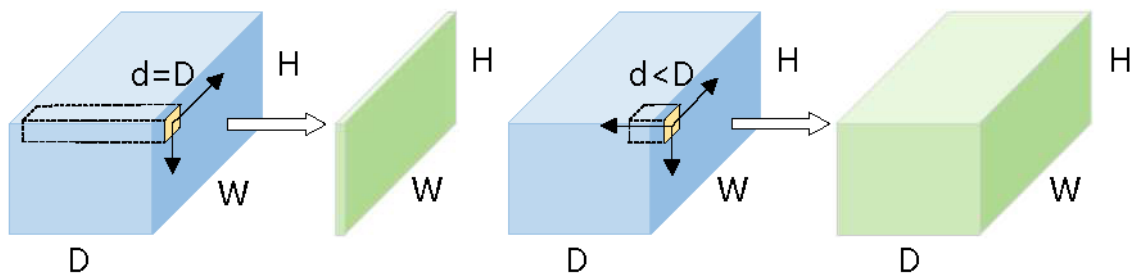
$$\tilde{\mathbf{x}}_k = \mathbf{z}_k - \mathbf{u}_k$$

$$\tilde{\mathbf{z}}_k = \mathbf{x}_{k+1} + \mathbf{u}_k$$

Deep denoiser

Hybrid Strategies for Hyperspectral Deconvolution

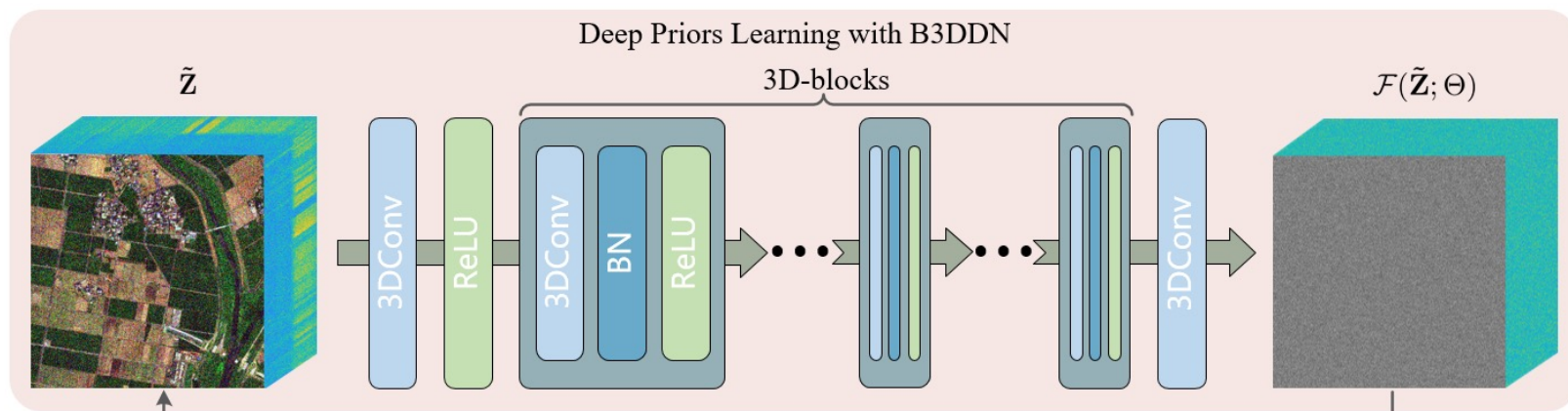
Deep denoiser:



Difference between 2D and 3D convolution

Two advantages:

- Operate locally in Spectral domain
- Involve fewer kernel parameters



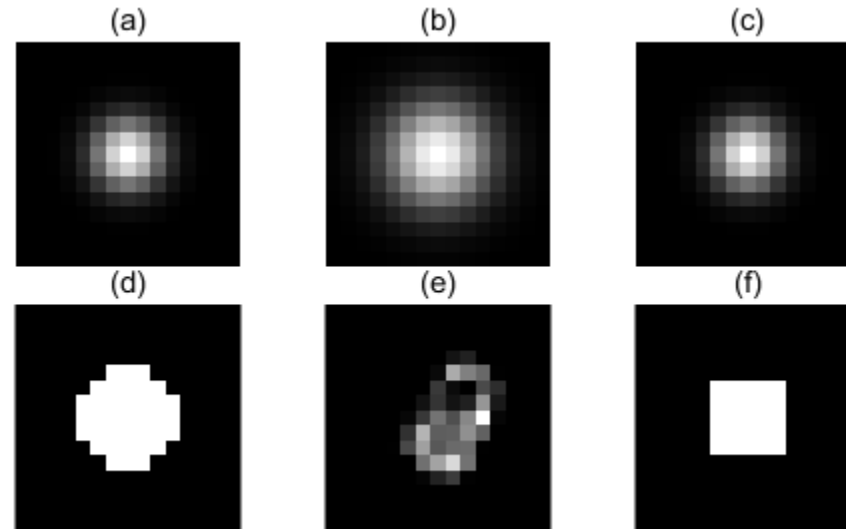
Architecture of the proposed B3DDN for hyperspectral image denoising

Loss function:

$$\ell(\Theta) = \|\mathcal{F}(\tilde{\mathbf{z}}_m; \Theta) - (\tilde{\mathbf{z}}_m - \mathbf{z}_m)\|_1$$

Hybrid Strategies for Hyperspectral Deconvolution

Experiments:



Blurring kernels used in the experiments

Baselines:

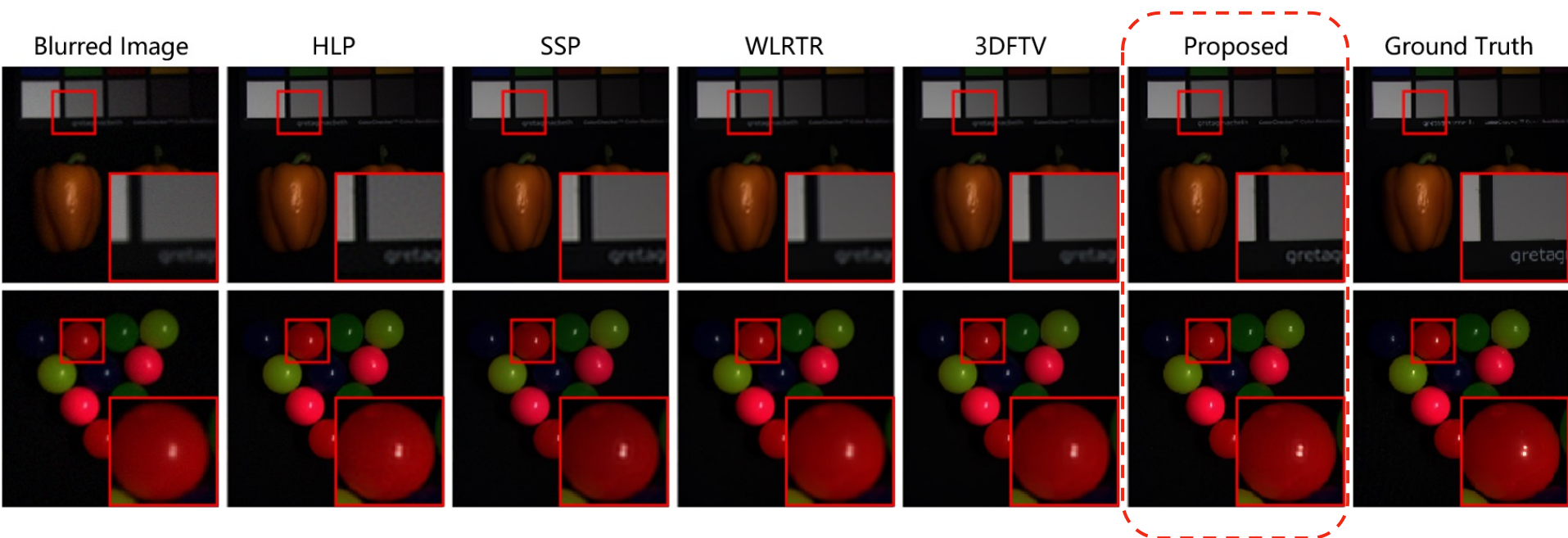
- HLP: considers the spatial smoothness;
- SSP: exploits both the spatial and spectral smoothness;
- WLRTR: captures non-local similarity and spectral correlation;
- 3DFTV: exploits smoothness of images in all dimensions.

Hybrid Strategies for Hyperspectral Deconvolution

Scenarios	Metrics	HLP	SSP	WLRTR	3DFTV	Ours
(a)	RMSE	4.420 $\pm$ 1.787	4.848 $\pm$ 1.825	4.735 $\pm$ 2.076	4.332 $\pm$ 1.863	3.132 $\pm$ 1.320
	PSNR	36.166 $\pm$ 3.334	35.373 $\pm$ 3.385	35.872 $\pm$ 3.759	36.450 $\pm$ 3.793	39.252 $\pm$ 3.465
	SSIM	0.9167 $\pm$ 0.0379	0.9305 $\pm$ 0.0393	0.9380 $\pm$ 0.0466	0.9401 $\pm$ 0.0439	0.9493 $\pm$ 0.0367
	ERGAS	18.15 $\pm$ 8.25	19.51 $\pm$ 8.12	18.96 $\pm$ 8.33	17.34 $\pm$ 7.69	13.01 $\pm$ 6.23
(b)	RMSE	5.707 $\pm$ 2.452	5.955 $\pm$ 2.398	6.439 $\pm$ 2.812	5.667 $\pm$ 2.539	4.581 $\pm$ 1.993
	PSNR	34.034 $\pm$ 3.567	33.541 $\pm$ 3.492	33.084 $\pm$ 3.740	34.116 $\pm$ 3.872	36.305 $\pm$ 3.612
	SSIM	0.8911 $\pm$ 0.0483	0.9031 $\pm$ 0.0494	0.9025 $\pm$ 0.0616	0.9136 $\pm$ 0.550	0.9234 $\pm$ 0.0422
	ERGAS	22.92 $\pm$ 10.11	23.71 $\pm$ 9.86	25.46 $\pm$ 10.84	22.40 $\pm$ 9.86	18.54 $\pm$ 8.39
(c)	RMSE	7.669 $\pm$ 1.390	5.270 $\pm$ 1.622	5.099 $\pm$ 1.972	5.016 $\pm$ 1.727	4.225 $\pm$ 1.324
	PSNR	30.599 $\pm$ 1.550	34.309 $\pm$ 2.607	34.827 $\pm$ 3.201	34.741 $\pm$ 2.975	36.211 $\pm$ 2.485
	SSIM	0.6406 $\pm$ 0.0337	0.8565 $\pm$ 0.0539	0.8956 $\pm$ 0.0387	0.8851 $\pm$ 0.0390	0.8708 $\pm$ 0.0594
	ERGAS	33.49 $\pm$ 16.27	22.28 $\pm$ 10.14	20.80 $\pm$ 9.07	20.47 $\pm$ 8.66	18.64 $\pm$ 9.28
(d)	RMSE	4.189 $\pm$ 1.636	4.584 $\pm$ 1.680	4.328 $\pm$ 1.903	4.167 $\pm$ 1.803	2.305 $\pm$ 0.938
	PSNR	36.548 $\pm$ 3.181	35.862 $\pm$ 3.331	36.686 $\pm$ 3.736	36.805 $\pm$ 3.803	41.653 $\pm$ 3.074
	SSIM	0.9165 $\pm$ 0.0348	0.9354 $\pm$ 0.0374	0.9450 $\pm$ 0.0436	0.9403 $\pm$ 0.0430	0.9542 $\pm$ 0.0340
	ERGAS	17.36 $\pm$ 7.98	18.49 $\pm$ 7.67	17.45 $\pm$ 7.82	16.69 $\pm$ 7.46	9.86 $\pm$ 5.17
(e)	RMSE	3.759 $\pm$ 1.166	3.954 $\pm$ 1.333	4.335 $\pm$ 1.780	3.587 $\pm$ 1.443	3.041 $\pm$ 2.783
	PSNR	37.149 $\pm$ 2.492	37.160 $\pm$ 3.108	36.497 $\pm$ 3.490	37.991 $\pm$ 3.543	40.722 $\pm$ 5.730
	SSIM	0.9118 $\pm$ 0.0239	0.9472 $\pm$ 0.0311	0.9428 $\pm$ 0.0436	0.9510 $\pm$ 0.0397	0.8907 $\pm$ 0.1642
	ERGAS	15.94 $\pm$ 7.39	16.01 $\pm$ 6.56	17.46 $\pm$ 7.49	14.37 $\pm$ 6.16	15.56 $\pm$ 19.66
(f)	RMSE	3.971 $\pm$ 1.453	4.356 $\pm$ 1.563	4.109 $\pm$ 1.765	3.957 $\pm$ 1.666	2.280 $\pm$ 1.231
	PSNR	36.910 $\pm$ 2.985	36.322 $\pm$ 3.302	37.130 $\pm$ 3.698	37.225 $\pm$ 3.743	41.932 $\pm$ 3.687
	SSIM	0.9195 $\pm$ 0.0270	0.9397 $\pm$ 0.334	0.9480 $\pm$ 0.0450	0.9468 $\pm$ 0.0410	0.9475 $\pm$ 0.0618
	ERGAS	16.58 $\pm$ 7.61	17.60 $\pm$ 7.26	16.64 $\pm$ 7.46	15.89 $\pm$ 7.04	9.79 $\pm$ 5.89

Quantitative comparison

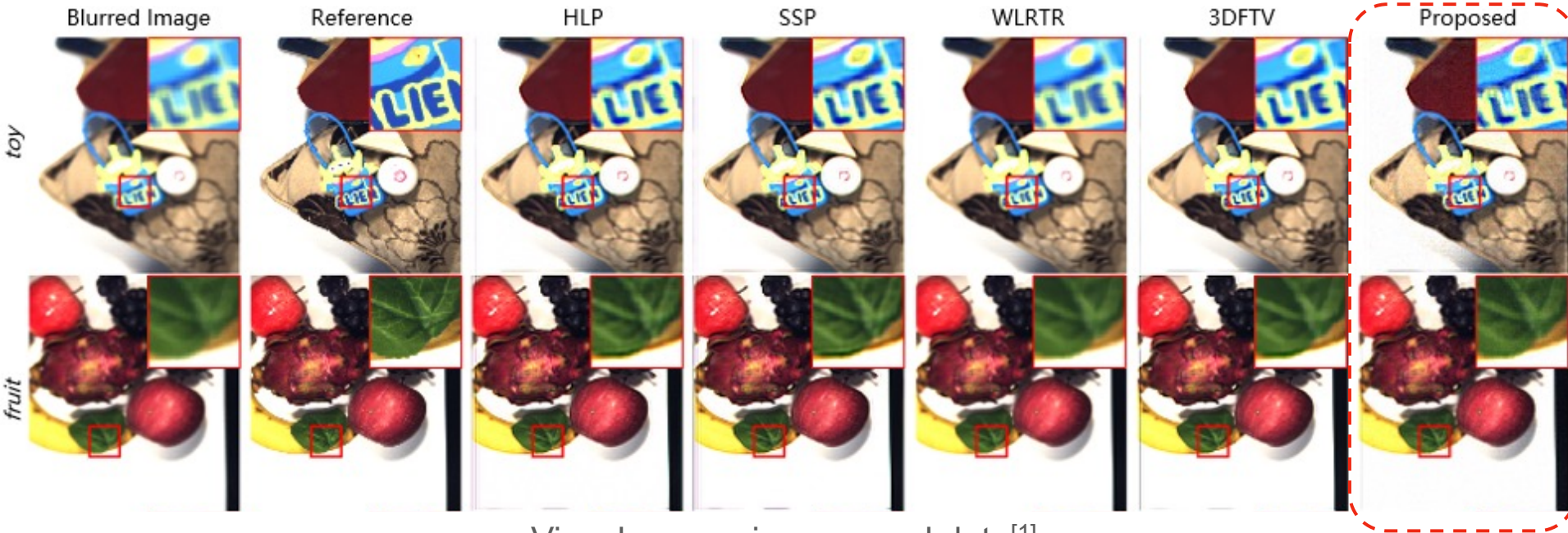
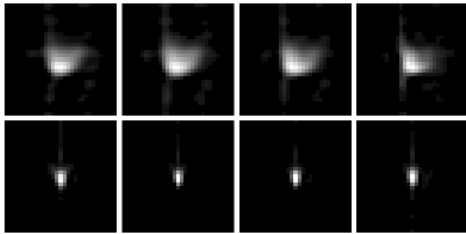
Hybrid Strategies for Hyperspectral Deconvolution



Visual comparison on synthetic data

Hybrid Strategies for Hyperspectral Deconvolution

Real data collection:



Visual comparison on real data^[1]

[1] Available at: https://github.com/xiuheng-wang/Tuning_free_PnP_HSI_deconvolution

Hybrid Strategies for Hyperspectral Deconvolution

Constrained optimization:

$$\hat{\mathbf{x}} = \arg \min_{\mathbf{x}} \frac{1}{2} \|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2 + \lambda \mathcal{R}(\mathbf{z}), \quad \text{s. t.} \quad \mathbf{z} = \mathbf{x}.$$

Augmented Lagrangian :

$$\mathcal{L}_{\rho}(\mathbf{x}, \mathbf{z}, \mathbf{v}) = \arg \min_{\mathbf{x}} \frac{1}{2} \|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2 + \lambda \Phi(\mathbf{z}) + \frac{\rho}{2} \|\mathbf{x} - \mathbf{z}\|^2.$$

Variable splitting based on HQS^[1]:

$$\begin{aligned} \mathbf{z}_{k+1} &= \arg \min_{\mathbf{z}} \lambda \Phi(\mathbf{z}) + \frac{\rho}{2} \|\mathbf{x}_k - \mathbf{z}\|^2 \\ \mathbf{x}_{k+1} &= \arg \min_{\mathbf{x}} \frac{1}{2} \|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2 + \frac{\rho}{2} \|\mathbf{x} - \mathbf{z}_{k+1}\|^2 \end{aligned}$$



$$\begin{aligned} \mathbf{z}_{k+1} &= \text{denoiser}(\mathbf{x}_k, \Theta_k) \\ \mathbf{x}_{k+1} &= (\mathbf{H}^T \mathbf{H} + \rho \mathbf{I})^{-1} (\mathbf{H}^T \mathbf{y} + \rho \mathbf{z}_{k+1}) \end{aligned}$$

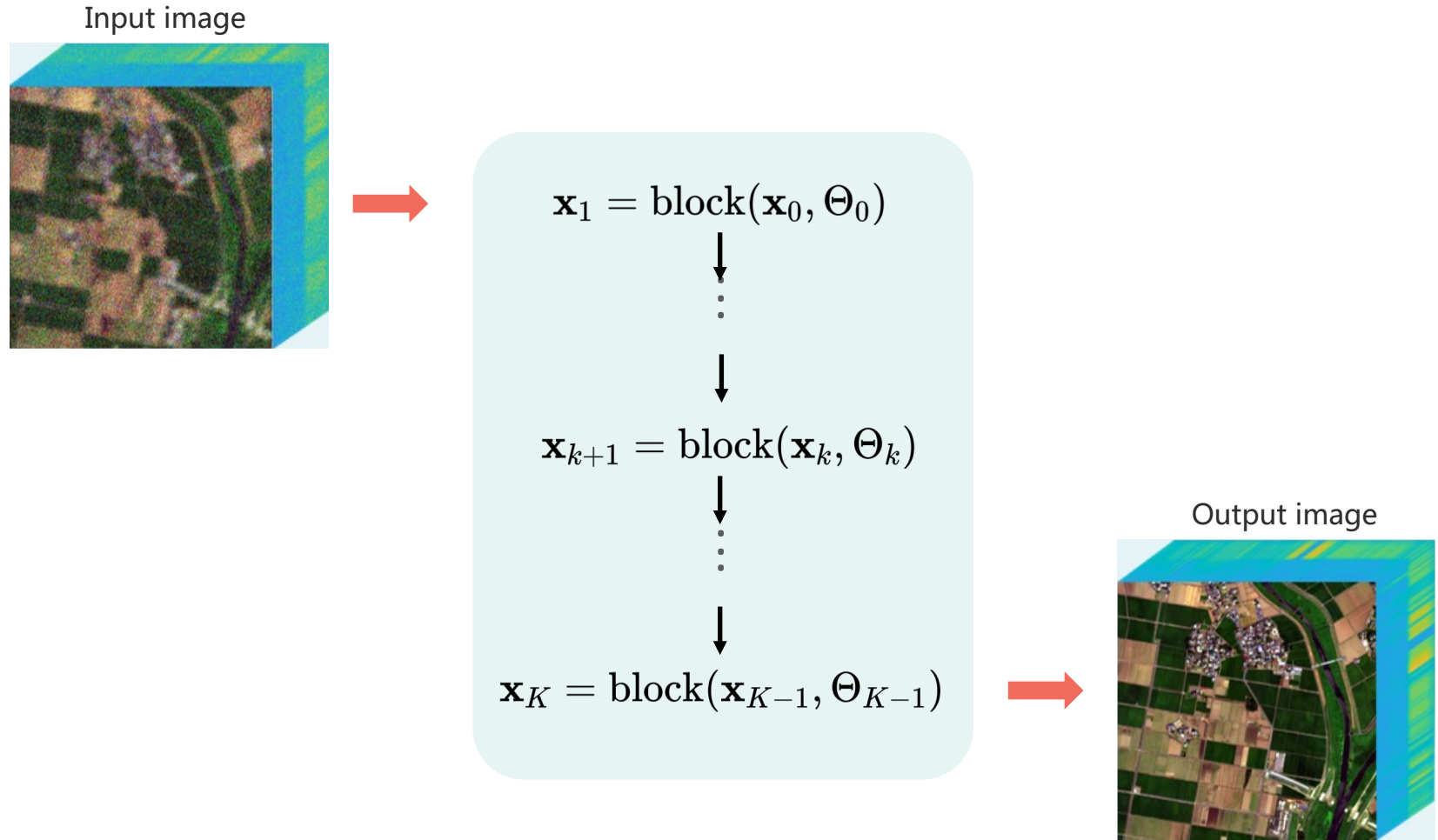


$$\mathbf{x}_{k+1} = \text{block}(\mathbf{x}_k, \Theta_k)$$

[1] A. Gkillas, D. Ampeliotis, and K. Berberidis, "A highly interpretable deep equilibrium network for hyperspectral image deconvolution," in ICASSP, 2023, pp. 1–5.

Hybrid Strategies for Hyperspectral Deconvolution

Deep unrolling framework^[1]:



[1] A. Gkillas, D. Ampeliotis, and K. Berberidis, "A highly interpretable deep equilibrium network for hyperspectral image deconvolution," in ICASSP, 2023, pp. 1–5.

Hybrid Strategies for Hyperspectral Deconvolution

Experimental result^[2]:

Plug-and-play^[1] deep unrolling^[2]

(a)	PSNR	41.17	41.78
	SSIM	0.9602	0.9793
	SAM	6.27	5.94
(b)	PSNR	35.96	38.51
	SSIM	0.9199	0.9647
	SAM	7.77	6.68
(c)	PSNR	37.42	39.65
	SSIM	0.9395	0.9678
	SAM	6.46	6.13
(d)	PSNR	39.88	41.77
	SSIM	0.9477	0.9801
	SAM	6.80	6.01
(e)	PSNR	42.71	45.21
	SSIM	0.9669	0.9884
	SAM	6.29	5.55

[1] X. Wang, J. Chen, C. Richard, and D. Brie, “Learning spectral-spatial prior via 3ddncnn for hyperspectral image deconvolution,” in ICASSP, 2020, pp. 2403–2407.

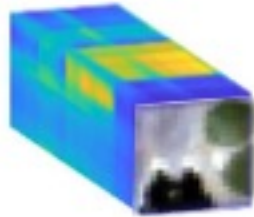
[2] A. Gkillas, D. Ampeliotis, and K. Berberidis, “A highly interpretable deep equilibrium network for hyperspectral image deconvolution,” in ICASSP, 2023, pp. 1–5.

Hybrid Strategies for Hyperspectral Deconvolution

Plug-and-play v.s. Deep unrolling:

	Plug-and-play	Deep unrolling
Flexibility	Very flexible, reusable denoiser	Less flexible, needs retraining
Task Specificity	Generic, not task-optimized	Task-specific, highly adapted
Data	No paired data needed	Requires paired training data
Inference Speed	Slow, many iterations	Fast, fixed number of layers
Performance	Not always optimal	Often state-of-the-art

Hybrid Strategies for Hyperspectral Fusion



Hyperspectral Image (HI):

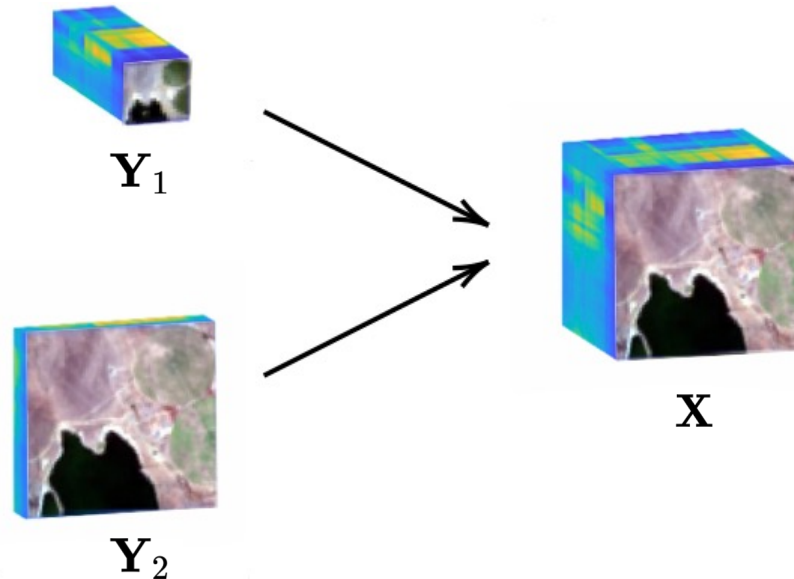
- Hundreds of spectral bands
- Low spatial resolution



Multispectral Image (MI):

- Very few spectral bands
- High spatial resolution

Hybrid Strategies for Hyperspectral Fusion



Linear degradation model:

$$\begin{aligned} \mathbf{Y}_1 &= \mathbf{XBS} + \mathbf{N}_1, \\ \mathbf{Y}_2 &= \mathbf{RX} + \mathbf{N}_2. \end{aligned}$$

The optimization problem:

$$\hat{\mathbf{X}} = \arg \min_{\mathbf{X}} \left\{ \|\mathbf{Y}_1 - \mathbf{XBS}\|_{\text{F}}^2 + \|\mathbf{Y}_2 - \mathbf{RX}\|_{\text{F}}^2 + \lambda \mathcal{R}(\mathbf{X}) \right\}.$$

Hybrid Strategies for Hyperspectral Fusion

Deep Prior Regularization^[1] :

$$\begin{aligned}\hat{\mathbf{X}} &= \arg \min_{\mathbf{X}} \left\{ \|\mathbf{Y}_1 - \mathbf{XBS}\|_F^2 + \|\mathbf{Y}_2 - \mathbf{RX}\|_F^2 + \lambda \mathcal{R}(\mathbf{X}) \right\} \\ &= \arg \min_{\mathbf{X}} \left\{ \|\mathbf{Y}_1 - \mathbf{XBS}\|_F^2 + \|\mathbf{Y}_2 - \mathbf{RX}\|_F^2 + \lambda \|\mathbf{X} - \tilde{\mathbf{X}}\|_F^2 \right\}\end{aligned}$$

This formulation allows a straight-forward solver^[2] with the optimum defined by

$$\mathbf{C}_1 \mathbf{X}^* + \mathbf{X}^* \mathbf{C}_2 = \mathbf{C}_3 ,$$

where

$$\mathbf{C}_1 = \mathbf{R}^T \mathbf{R} + \lambda \mathbf{I}_B$$

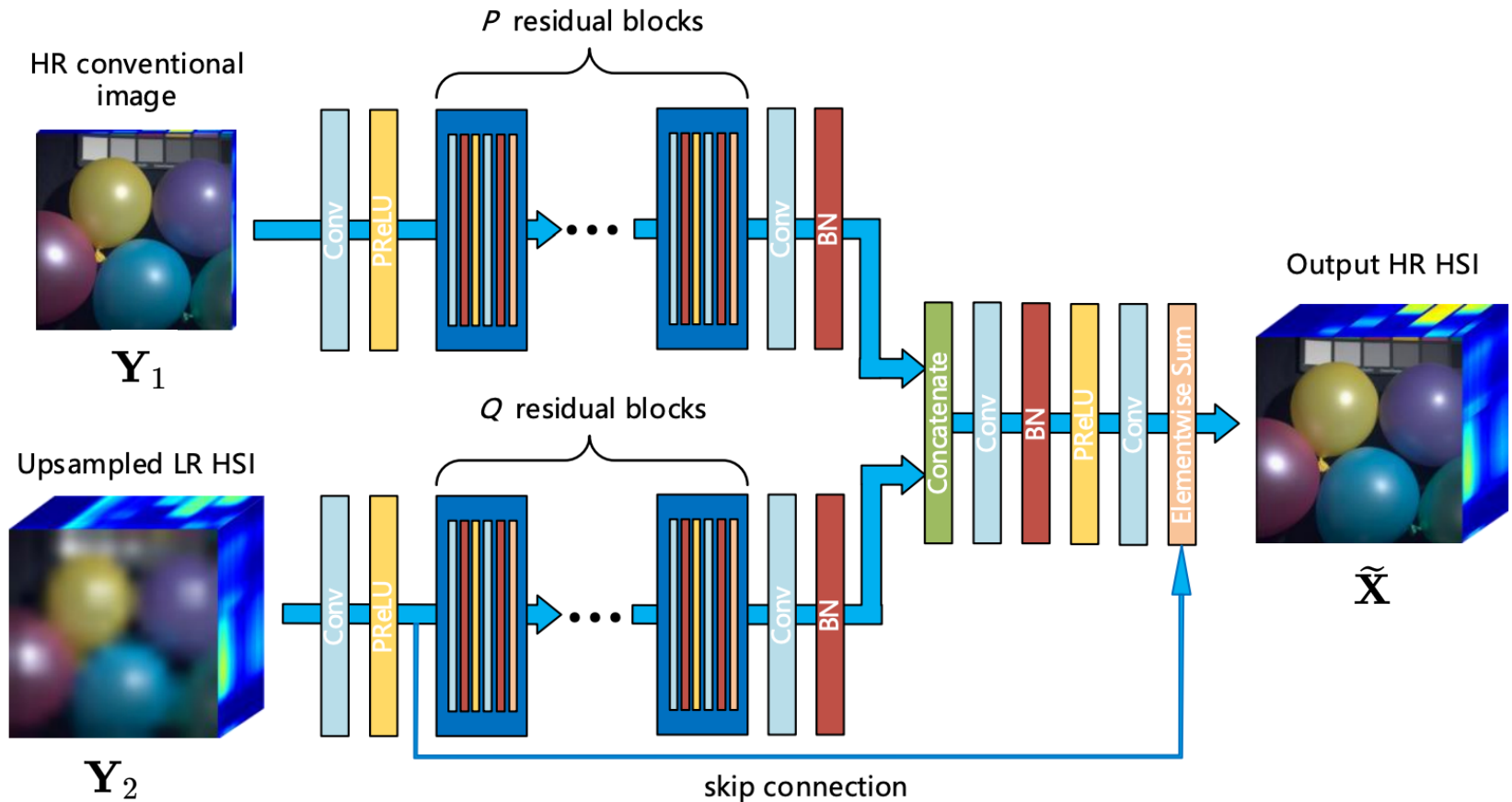
$$\mathbf{C}_2 = (\mathbf{BS})(\mathbf{BS})^T$$

$$\mathbf{C}_3 = \mathbf{R}^T \mathbf{Z} + \mathbf{Y}(\mathbf{BS})^T + \lambda \tilde{\mathbf{X}}$$

[1] X. Wang, J. Chen, Q. Wei, and C. Richard, "Hyperspectral image superresolution via deep prior regularization with parameter estimation," IEEE Trans. Circuits Syst. Video Technol., 2021.

[2] Q. Wei, N. Dobigeon, and J.-Y. Tournet, "Fast fusion of multi-band images based on solving a sylvester equation," IEEE Trans. Image Process., vol. 24, no. 11, pp. 4109–4121, 2015.

Hybrid Strategies for Hyperspectral Fusion



Architecture of the proposed TSFN for hyperspectral image fusion.

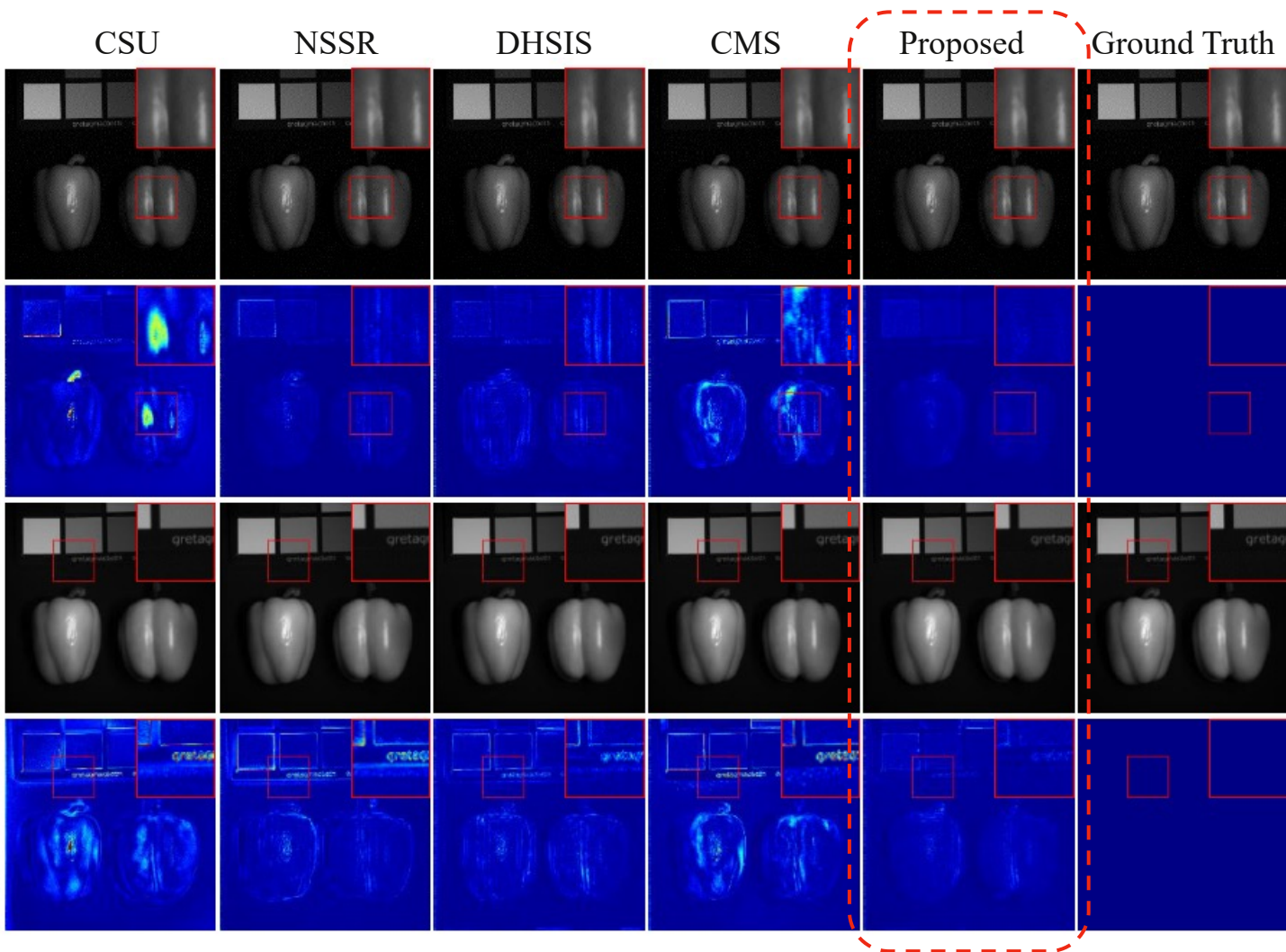
[1] X. Wang, J. Chen, Q. Wei, and C. Richard, "Hyperspectral image superresolution via deep prior regularization with parameter estimation," IEEE Trans. Circuits Syst. Video Technol., 2021.

Hybrid Strategies for Hyperspectral Fusion

	Metric	CSU	NSSR	DHSIS	CMS	LTTR	UAL	Proposed
$s = 8$	RMSE	2.57	1.47	1.36	1.65	1.49	1.42	1.12
	PSNR	41.76	46.66	47.01	45.29	46.55	46.47	48.63
	ERGAS	1.196	0.665	0.621	0.734	0.672	0.640	0.511
	SAM	6.27	3.72	3.74	3.89	3.84	3.60	3.23
$s = 16$	RMSE	2.82	1.77	1.79	1.99	1.84	1.57	1.39
	PSNR	41.01	45.31	44.74	43.94	44.87	45.80	47.02
	ERGAS	0.643	0.398	0.391	0.445	0.415	0.345	0.310
	SAM	6.47	4.32	4.57	4.37	4.63	3.84	3.76
$s = 32$	RMSE	3.02	2.24	2.45	2.35	2.28	1.85	1.80
	PSNR	40.44	43.49	42.34	42.66	43.33	44.66	45.07
	ERGAS	0.336	0.244	0.257	0.257	0.248	0.196	0.190
	SAM	6.83	5.22	5.87	5.04	5.46	4.33	4.59

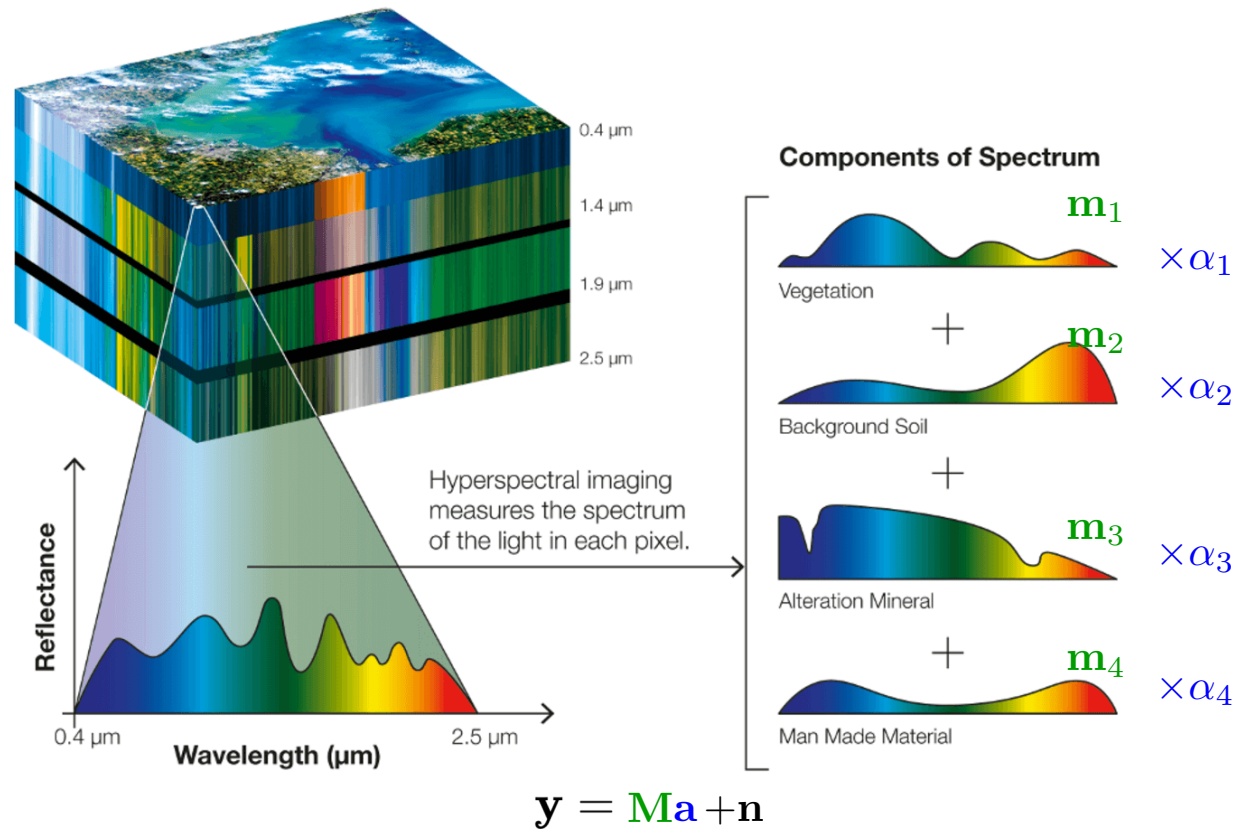
Quantitative comparison

Hybrid Strategies for Hyperspectral Fusion



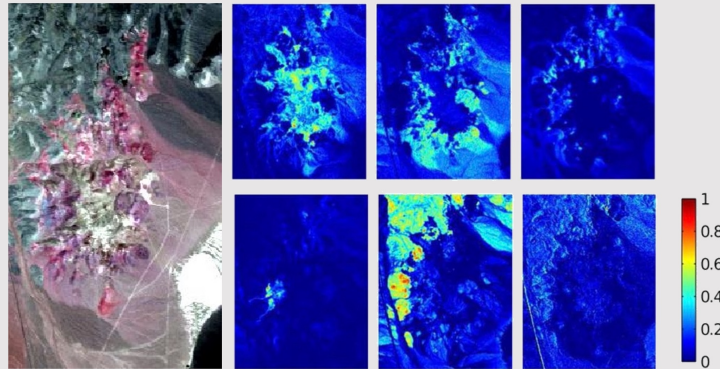
Visual comparison

Hybrid Strategies for Hyperspectral Unmixing

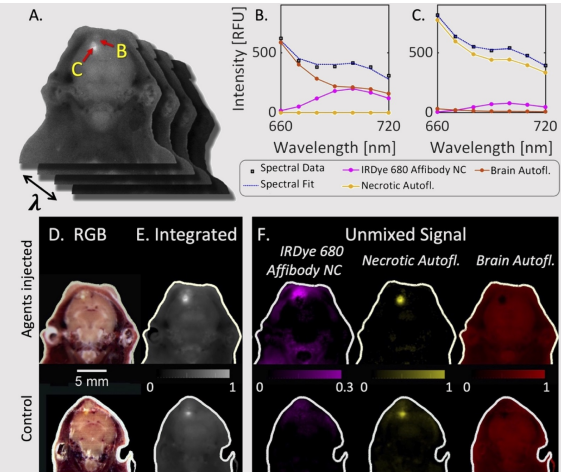


Hyperspectral unmixing aims at separating a mixed pixel into a set of endmembers and their corresponding abundances.

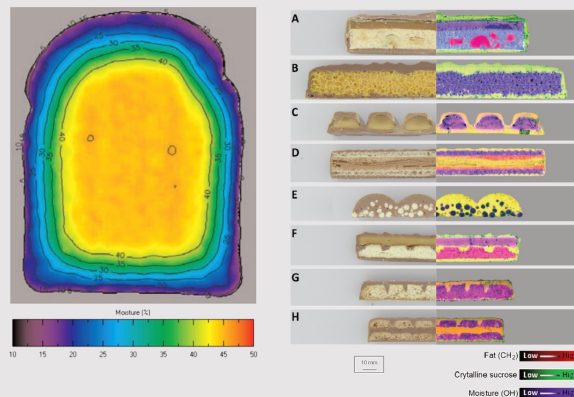
Hybrid Strategies for Hyperspectral Unmixing



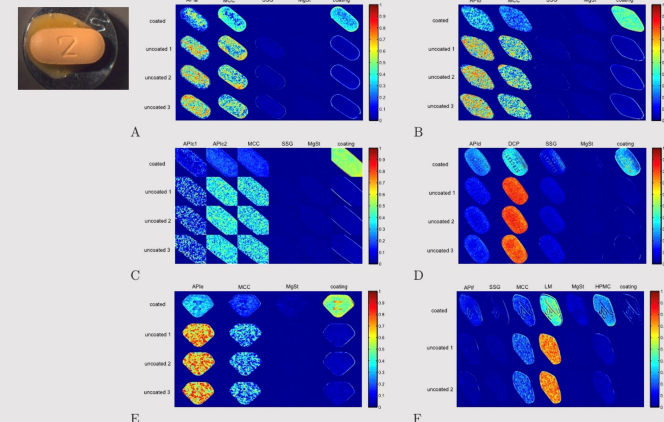
(a) Earth observation – minerals distribution analysis



(b) Animal fluorescence cryo-imaging analysis



(c) Food quality and composition analysis



(d) Pharmaceutical analysis – tablets ingredients

Applications of hyperspectral unmixing

Hybrid Strategies for Hyperspectral Unmixing

An observed spectrum can be described by

$$\mathbf{y} = \mathcal{F}^*(\mathbf{M}, \mathbf{a}) + \mathbf{n}$$

The constraints ANC and ASC are often considered:

$$\Omega_M = \{\mathbf{M} : \mathbf{M} \geq \mathbf{0}\}$$

$$\Omega_a = \{\mathbf{a} : \mathbf{a} \geq \mathbf{0}; a_1 + a_2 + \cdots + a_R = 1\}$$

Examples of physical mixture models^[1]

- Linear mixture model: $\mathbf{y} = \mathbf{M}\mathbf{a} + \mathbf{n}$
- Bilinear model: $\mathbf{y} = \mathbf{M}\mathbf{a} + \sum_{i=1}^R \sum_{j=1}^R \gamma_{i,j} \mathbf{m}_i \odot \mathbf{m}_j + \mathbf{n}$
- Additive nonlinear models: $\mathbf{y} = \mathbf{M}\mathbf{a} + \mathcal{F}_{\text{add}}(\mathbf{M}, \mathbf{a}) + \mathbf{n}$
- Post-nonlinear models: $\mathbf{y} = \mathcal{F}_{\text{post}}(\mathbf{M}, \mathbf{a}) + \mathbf{n}$

[1] J. Chen, M. Zhao, X. Wang, C. Richard and S. Rahardja, "Integration of physics-based and data-driven models for hyperspectral image unmixing: A summary of current methods". In: IEEE Signal Processing Magazine 40.2 (2023), pp. 61–74.

Hybrid Strategies for Hyperspectral Unmixing

Two examples of linear unmixing:

- The Fully Constrained Least Square (FCLS) problem^[1]:

$$\begin{aligned}\hat{\mathbf{a}} &= \underset{\mathbf{a}}{\operatorname{argmin}} \|\mathbf{y} - \mathbf{M}\mathbf{a}\|^2 \\ \text{s.t. } &\mathbf{a} \in \Omega_{\alpha}.\end{aligned}$$

- The regularized NMF unmixing^[2]:

$$\begin{aligned}\{\hat{\mathbf{M}}, \{\hat{\mathbf{a}}_i\}_{i=1}^N\} &= \underset{\mathbf{M}, \{\mathbf{a}_i\}_{i=1}^N}{\operatorname{argmin}} \|\mathbf{Y} - \mathbf{M}\mathbf{A}\|_F^2 + \mathcal{R}(\mathbf{M}, \{\mathbf{a}_i\}_{i=1}^N) \\ \text{s.t. } &\mathbf{M} \in \Omega_M, \text{ and } \mathbf{a}_i \in \Omega_a,\end{aligned}$$

[1] D. Heinz and C. Chang, “Fully constrained least squares linear spectral mixture analysis method for material quantification in hyperspectral imagery,” *IEEE Trans. Geosci. Remote Sens.*, vol. 39, no. 3, pp. 529–545, 2001.

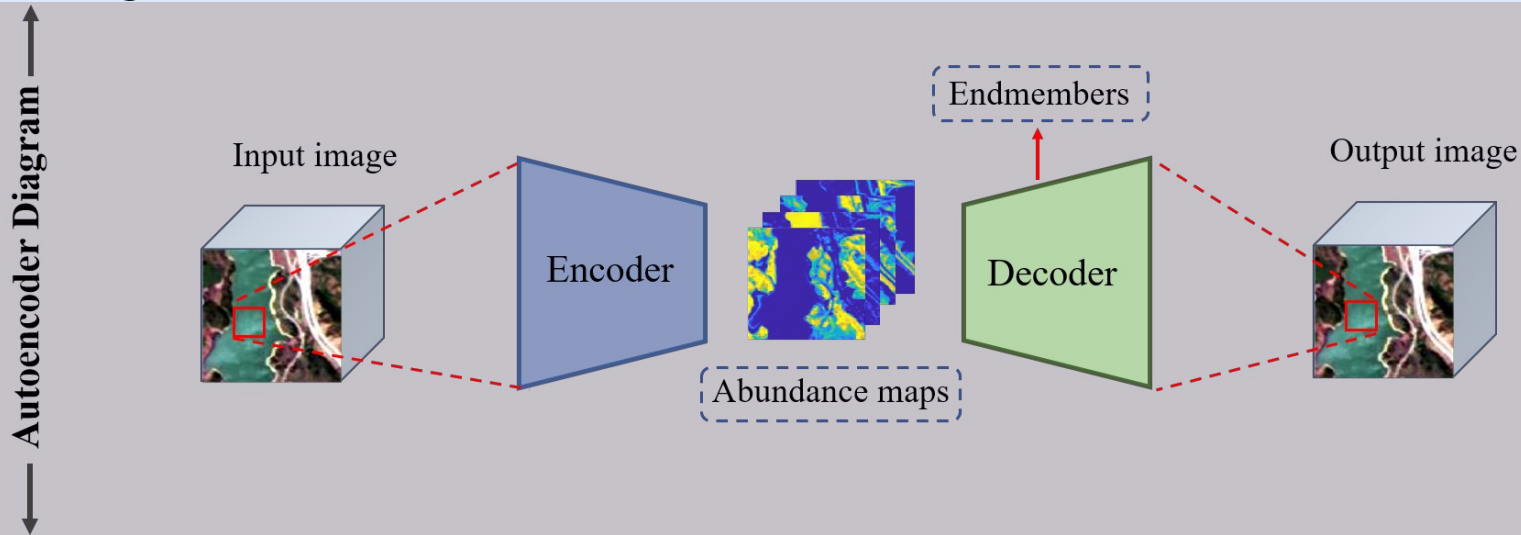
[2] J. Peng, W. Sun, H. Li, W. Li, X. Meng, C. Ge, and Q. Du, “Low-rank and sparse representation for hyperspectral image processing: A review,” *IEEE Geosci. Remote Sens. Mag.*, vol. 10, no. 1, pp. 10–43, 2021.

Hybrid Strategies for Hyperspectral Unmixing

$$\{\hat{\mathbf{x}}, \Theta^*\} = \arg \min_{\mathbf{x}, \Theta, \mathcal{F}} \{\mathcal{L}(\hat{\mathbf{y}}, \mathbf{y}) + \mathcal{R}(\mathbf{x})\}$$

with $\hat{\mathbf{y}} = \mathcal{F}(\mathbf{x}(\Theta)).$

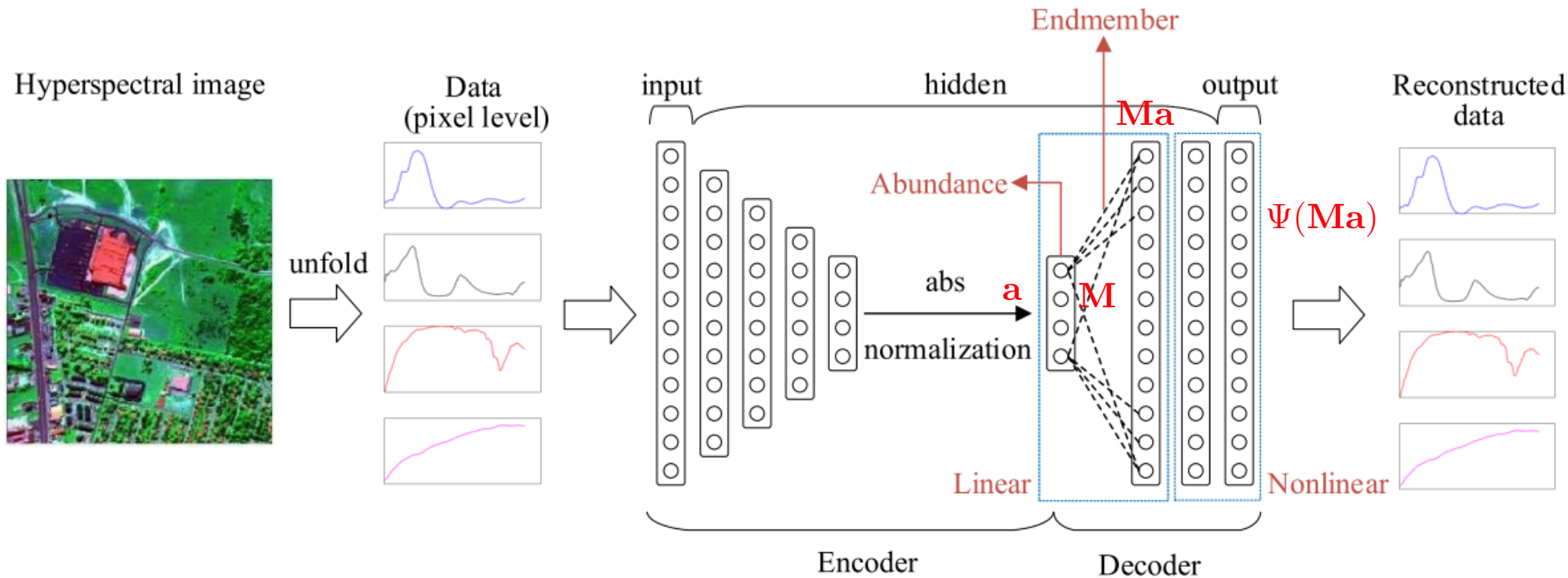
Deep autoencoder based unmixing DNNs preserve physical interpretation by modeling the spectral mixture mechanism^[1].



- **Encoder** seeks for a low dimensional representation (i.e., abundances);
- **Decoder** contains endmember information and reconstructs the input.

Hybrid Strategies for Hyperspectral Unmixing

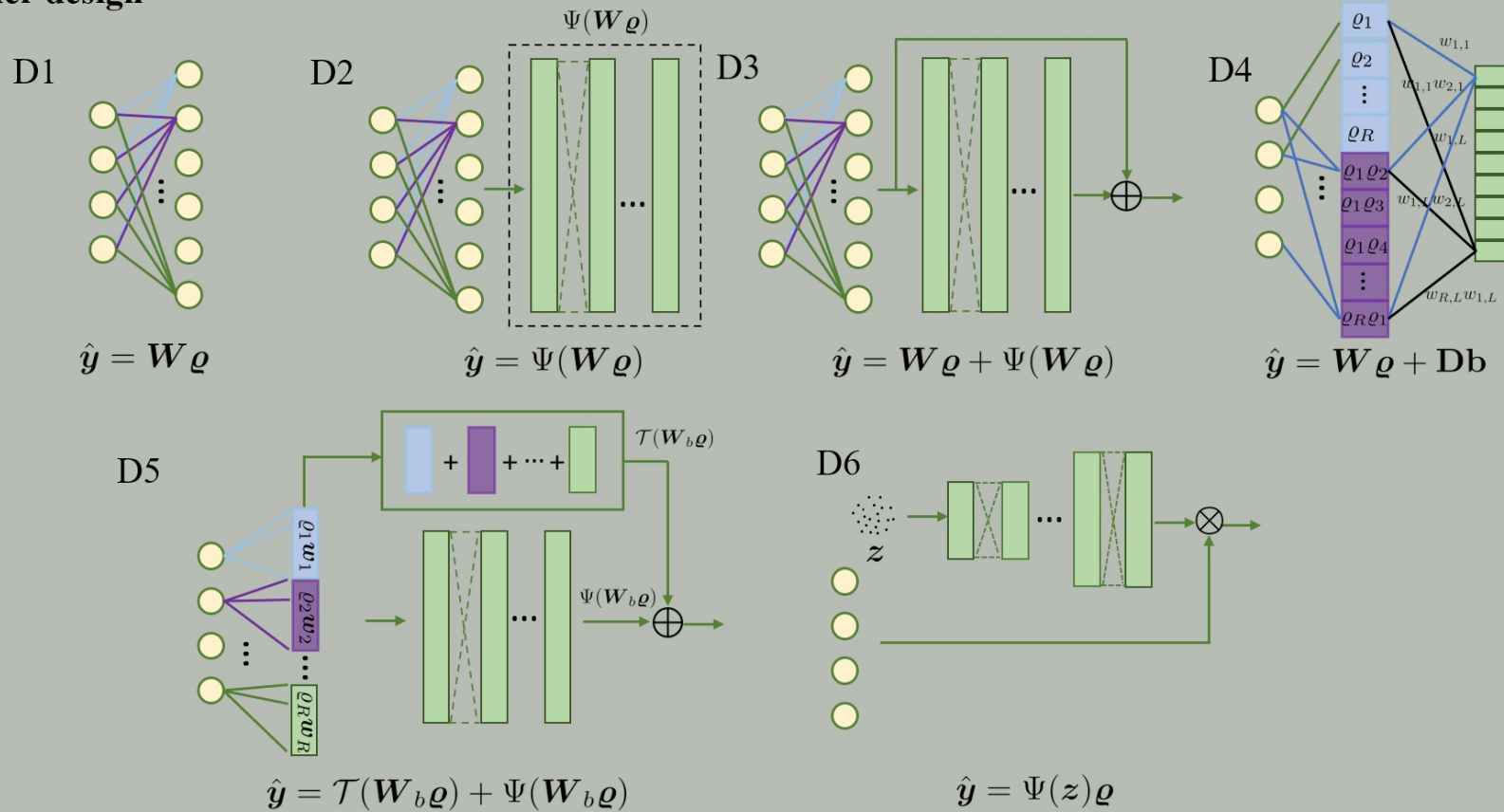
An example^[1]:



[1] M. Wang, M. Zhao, J. Chen, and S. Rahardja, "Nonlinear unmixing of hyperspectral data via deep autoencoder networks," IEEE Geosci. Remote Sens. Lett., vol. 16, no. 9, pp. 1467–1471, 2019.

Hybrid Strategies for Hyperspectral Unmixing

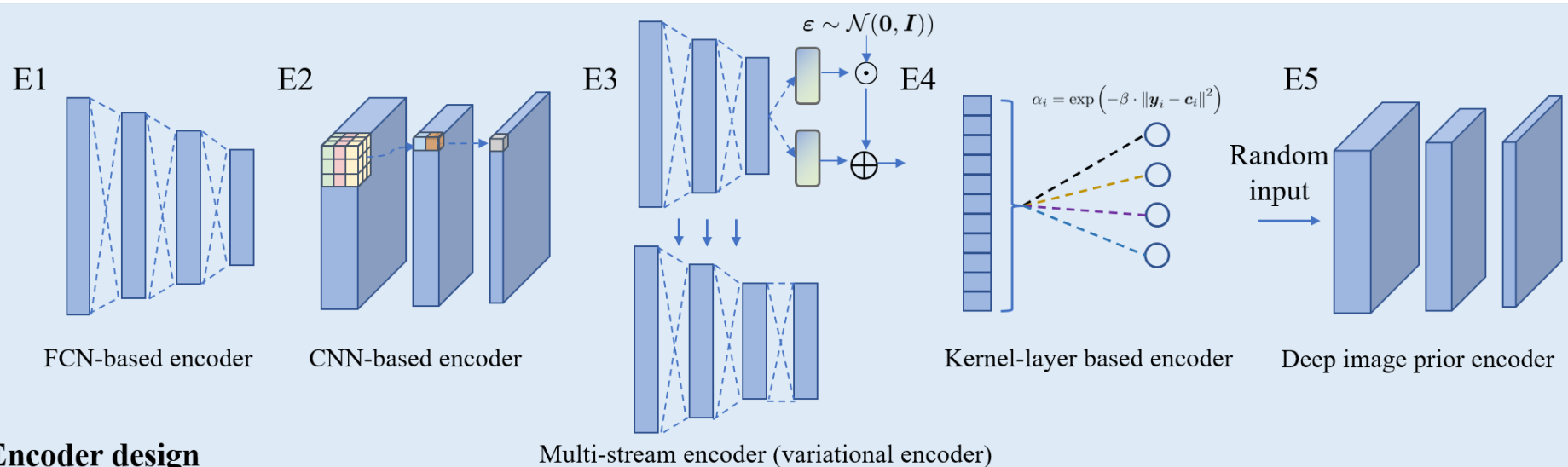
Decoder design



Design of decoders to learn models from data

Hybrid Strategies for Hyperspectral Unmixing

Separately show the design of encoders and decoders, to illustrate their extra flexibility and combination potential.



Design of encoders to learn priors from data

Hybrid Strategies for Hyperspectral Unmixing

Examples:

- **E2 + D5:** The 3D-CNN based autoencoder network for additive nonlinearity unmixing^[1];
- **E1 + D1:** A denoising autoencoder with sparsity for spectral unmixing^[2];
- **E4 + D3/D4:** The kernelization and cross product layer based autoencoder for bilinear and post nonlinearity unmixing^[3];
- **E3 + D6:** The probabilistic generative model based autoencoder for spectral unmixing with spectral variability^[4].

[1] M. Zhao, M. Wang, J. Chen, and S. Rahardja, “Hyperspectral Unmixing for Additive Nonlinear Models With a 3-D-CNN Autoencoder Network”. In: IEEE Trans. Geosci. Remote Sens. 60 (2022), 1–15.

[2] Y. Qu and H. Qi, “uDAS: An untied denoising autoencoder with sparsity for spectral unmixing”. In: IEEE Trans. Geosci. Remote Sens. 57.3 (2018), pp. 1698–1712.

[3] K. T. Shahid and I. D. Schizas, “Unsupervised Hyperspectral Unmixing via Nonlinear Autoencoders”. In: IEEE Trans. Geosci. Remote Sens. 60 (2021), 1–13.

[4] S. Shi, M. Zhao, L. Zhang, Y. Altmann, and J. Chen, “Probabilistic Generative Model for Hyperspectral Unmixing Accounting for Endmember Variability”. In: IEEE Trans. Geosci. Remote Sens. 60 (2022), 1–15.

Outline

Introduction

Part I: Methodology

- General Problem Formulation

- Hybrid Approaches for Parameter Estimation

- State-of-the-Art Hybrid Techniques

Part II: Applications to Image Processing

- Background in Hyperspectral Imaging

- Hybrid Strategies for Hyperspectral Deconvolution

- Hybrid Strategies for Hyperspectral Fusion

- Hybrid Strategies for Hyperspectral Unmixing

Part III: Applications to Speech Signal Processing

- Background in Speech Processing

- Hybrid Strategies for Speech Dereverberation

- Hybrid Strategies for Speech Separation

Summary and Future Directions

Applications in speech processing

■ Background



Colin Cherry (1953)



Cocktail party problem

- How can machines, like humans, robustly recognize a target speaker's speech in the presence of **multiple interferences**?

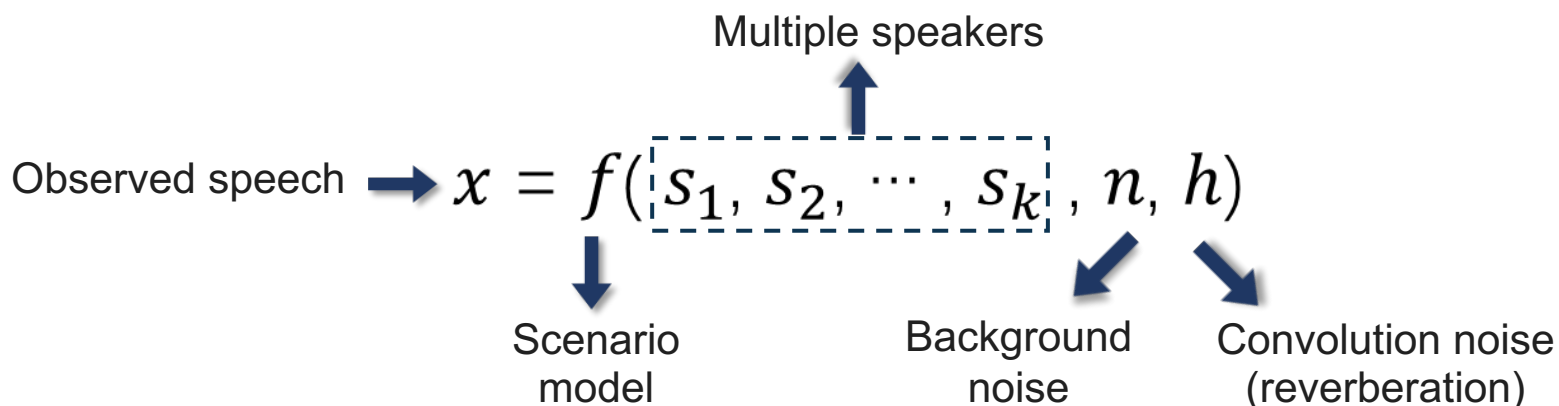
▶▶ Background noise

▶▶ Reverberation

▶▶ Multiple speaker

Applications in speech processing

- **Problem definition -- In complex acoustic scenarios with multiple people interacting**



- When $K=1$, only background noise exists, the problem degenerates into **speech denoising**.

$$x = f(s, y) \approx s + y$$

- When $K=1$, only convolutional noise exists, the problem degenerates into **speech dereverberation**. | ✓

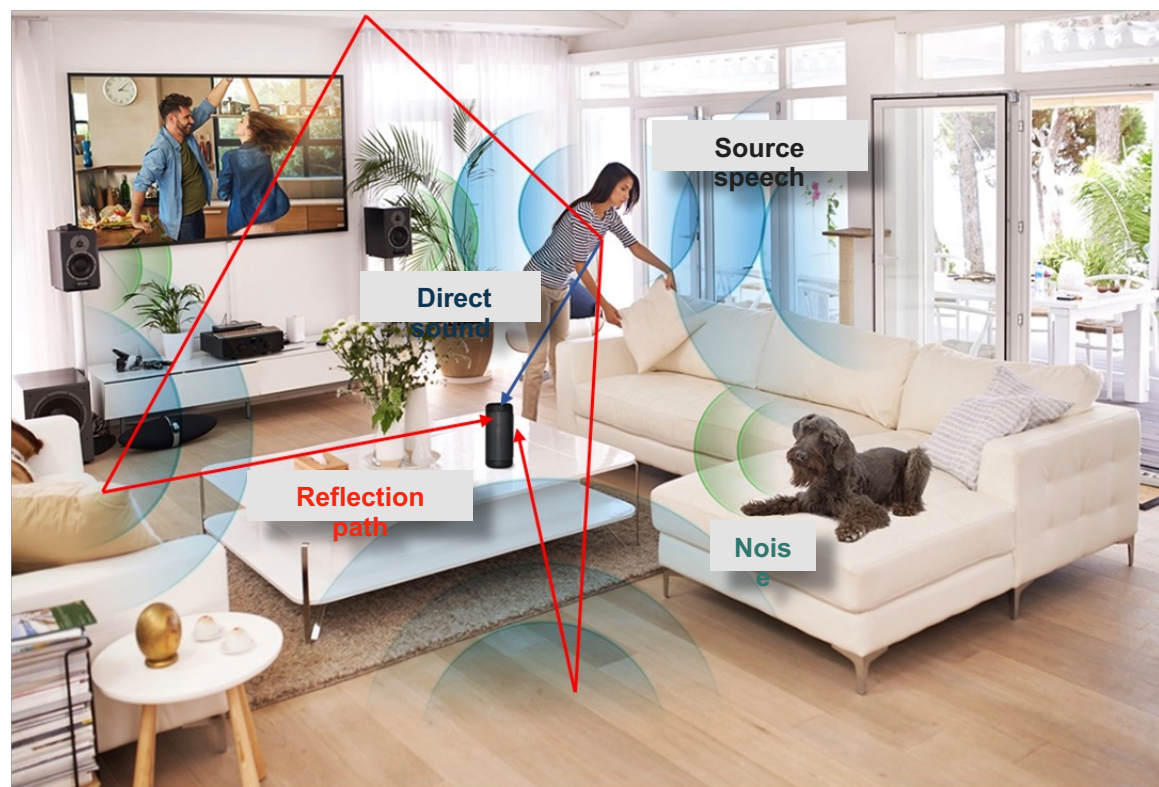
$$x = f(s, h) \approx s * h$$

- When $K>1$, with no noise interference, the problem degenerates into **speech separation**. | ✓

$$x = f(s_1, s_2, \dots, s_k) \approx s_1 + s_2 + \dots + s_k$$

Application in speech dereverberation

■ Reverberation causes



Direct Sound

- The **shortest path** from the sound source to the microphone
- Preserves speech clarity and localization information

Early Reflections

- First few reflections from walls, floor, and ceiling
- **Arrival delay < 50 ms**

Late reverberation

- Residual energy accumulated from multiple reflections
- **Arrival delay > 50 ms:** forms a “reverberant tail”.

Application in speech dereverberation

Early reflections

- Improves speech quality and intelligibility, contributing to a sense of envelopment.

Late Reverberation

- Causes spectral overlap of speech signals, reducing intelligibility.



The goal of speech dereverberation

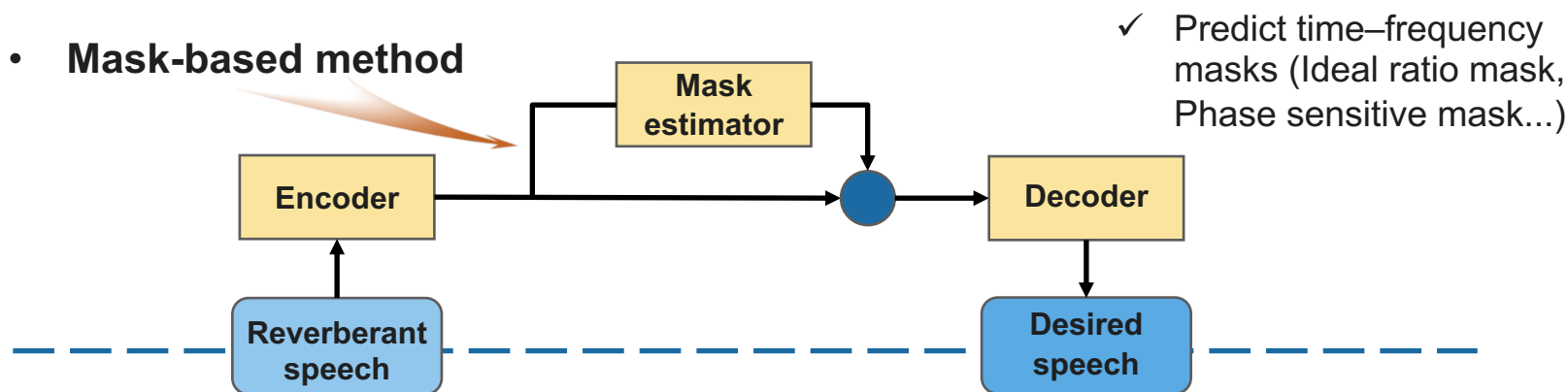
- Remove **late reverberation components**
- preserving the direct sound and early reverberation components.

Application in speech dereverberation

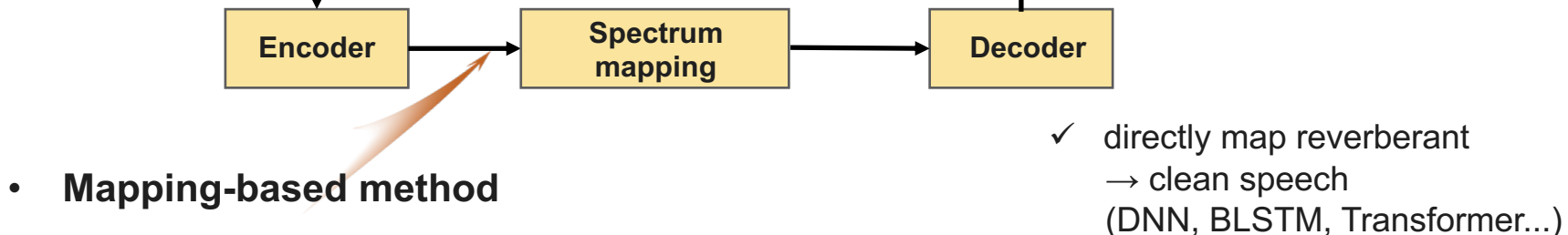
■ Speech dereverberation with data-driven methods

➤ Supervised learning problem

• Mask-based method



• Mapping-based method



➤ Challenges

- ✓ Generalization across rooms, speakers, and devices
- ✓ Limited real-world paired training data
- ✓ Reverberation often co-occurs with noise → overlap with speech denoising

Application in speech dereverberation

■ Speech dereverberation with physics-based method

- Addresses the dereverberation problem based on the speech convolution model

• Single-channel

- ✓ Acoustic channel equalization-based approach

- ✓ Deconvolution approach
(RIR is known)

• Multi-channel

- ✓ Beamforming approach

- ✓ Multi-channel linear prediction approach

Application in speech dereverberation

■ Speech Dereverberation with Deconvolution Regularized by Denoising

- Signal model is given by $x(t) = h(t) * s(t) + y(t) \rightarrow \mathbf{x} = \mathbf{H}\mathbf{s} + \mathbf{y}$
- The fidelity term of dereverberation process can be formulated by an inverse problem

$$\min_{\mathbf{s}} \|\mathbf{x} - \mathbf{H}\mathbf{s}\|^2$$

Even with $\mathbf{H}$ available, single-channel noise remains an *ill-posed problem*

$$\mathbf{H} = \begin{bmatrix} h_0 & h_{N-1} & \cdots & h_2 & h_1 \\ h_1 & h_0 & \cdots & \cdots & h_2 \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ h_{N-2} & h_{N-3} & \cdots & h_0 & h_{N-1} \\ h_{N-1} & h_{N-2} & \cdots & h_1 & h_0 \end{bmatrix}$$

- Incorporate the regularization term to stabilize the solution process

$$\min_{\mathbf{s}} \|\mathbf{y} - \mathbf{H}\mathbf{s}\|^2 + \boxed{\mathcal{R}(\mathbf{s}) \text{ Regularization term}}$$

RED: $\mathcal{R}(\mathbf{s}) = \frac{1}{2} \langle \mathbf{s}, \mathbf{s} - f(\mathbf{s}) \rangle$

$$\min_{\mathbf{s}} \|\mathbf{x} - \mathbf{H}\mathbf{s}\|^2 + \frac{\beta}{2} \mathbf{z}^\top (\boxed{\mathbf{z}} - f(\mathbf{z}))$$

Auxiliary variable

s.t. $\mathbf{z} = \mathbf{s}.$

Application in speech dereverberation

■ Speech Dereverberation with Deconvolution Regularized by Denoising

- Signal model is given by $x(t) = h(t) * s(t) + y(t) \longrightarrow \mathbf{x} = \mathbf{H}\mathbf{s} + \mathbf{y}$
- The fidelity term of dereverberation process can be formulated by an inverse problem

$$\min_{\mathbf{s}} \|\mathbf{x} - \mathbf{H}\mathbf{s}\|^2$$

Even with $\mathbf{H}$ available, single-channel observation under additive noise remains an *ill-posed problem*.

- Incorporate the regularization term to stabilize the solution process

$$\min_{\mathbf{s}} \|\mathbf{y} - \mathbf{H}\mathbf{s}\|^2 + \boxed{\mathcal{R}(\mathbf{s}) \text{ Regularization term}}$$

RED: $\mathcal{R}(\mathbf{s}) = \frac{1}{2} \langle \mathbf{s}, \mathbf{s} - \mathbf{f}(\mathbf{s}) \rangle \longrightarrow \min_{\mathbf{s}} \|\mathbf{x} - \mathbf{H}\mathbf{s}\|^2 + \frac{\beta}{2} \mathbf{z}^\top (\mathbf{z} - \mathbf{f}(\mathbf{z}))$

s.t. $\mathbf{z} = \mathbf{s}$. Auxiliary variable

Application in speech dereverberation

■ Tackle the problem via the Half-Quadratic Splitting (HQS) algorithm

$$\mathcal{L}(\mathbf{s}, \mathbf{z}) = \|\mathbf{x} - \mathbf{H}\mathbf{s}\|^2 + \frac{\rho}{2} \|\mathbf{s} - \mathbf{z}\|^2 + \frac{\beta}{2} \mathbf{z}^\top (\mathbf{z} - f(\mathbf{z}))$$

◆ With respect to $\mathbf{s}$:

$$\mathbf{s}^{(\ell+1)} = \arg \min_{\mathbf{s}} \|\mathbf{x} - \mathbf{H}\mathbf{s}\|^2 + \frac{\rho}{2} \|\mathbf{s} - \mathbf{z}^{(\ell)}\|^2$$

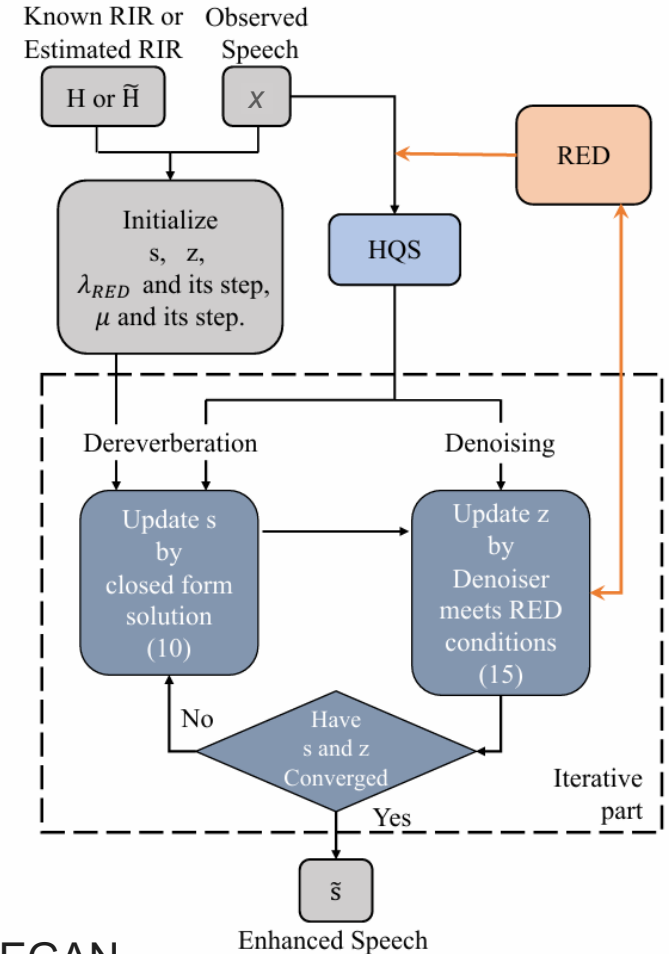
$$\mathbf{s}^{(\ell+1)} = (\mathbf{H}^\top \mathbf{H} + \frac{\rho}{2} \mathbf{I})^{-1} \left(\mathbf{H}^\top \mathbf{x} + \frac{\rho}{2} \mathbf{z}^{(n)} \right)$$

◆ With respect to $\mathbf{z}$:

$$\mathbf{z}^{(n+1)} = \arg \min_{\mathbf{z}} \frac{\rho}{2} \|\mathbf{s}^{(n+1)} - \mathbf{z}\|^2 + \frac{\beta}{2} \mathbf{z}^\top (\mathbf{z} - f(\mathbf{z}))$$

$$\mathbf{z}^{(\ell+1,i)} = \frac{\rho}{\rho + \beta} \mathbf{s}^{(\ell+1,i)} + \frac{\beta}{\rho + \beta} f(\mathbf{z}^{(\ell+1,i)})$$

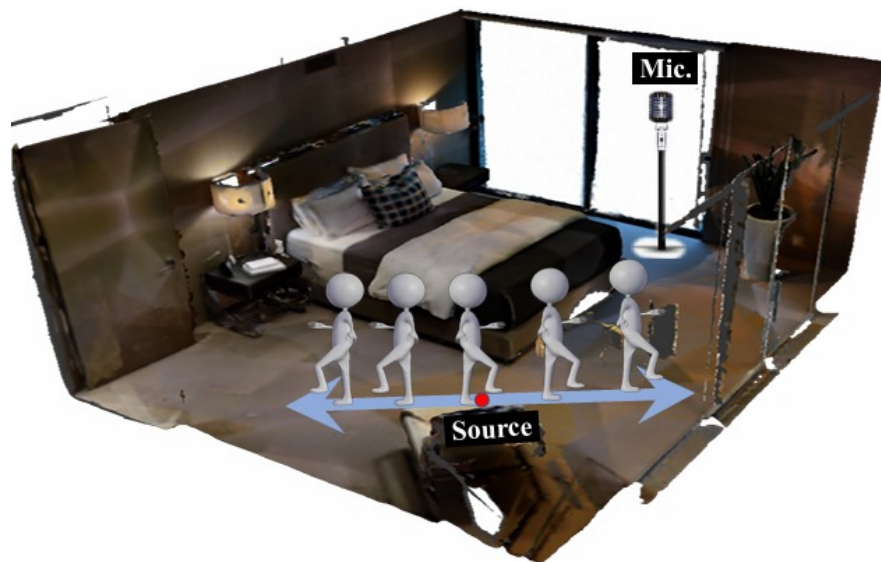
Pre-trained denoiser: SEGAN



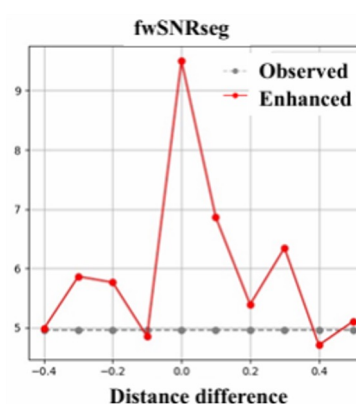
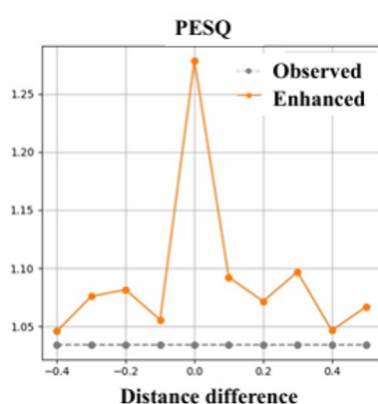
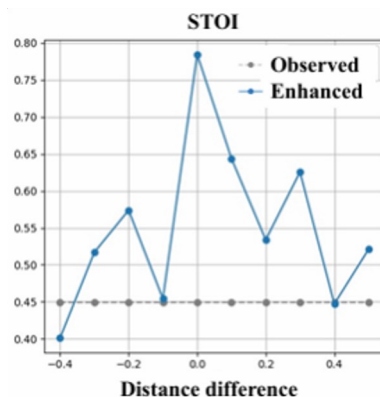
Application in speech dereverberation

■ Experiments

Simulated scenario of RIR positional mismatch based on SoundSpaces combined with Matterport3D



Room size	Randomly selected from the Matterport3D database
Clean speech corpus	Voice Bank corpus
RIR generation	SoundSpaces (ray tracing)
Source–microphone position	Random placement
T60 values	Approximately 190, 430, 890 ms (set around target values)
Noise levels	0, 10, 20 dB (White Gaussian Noise)
RIR mismatch introduction	Fix the microphone and move the source to simulate positional shift



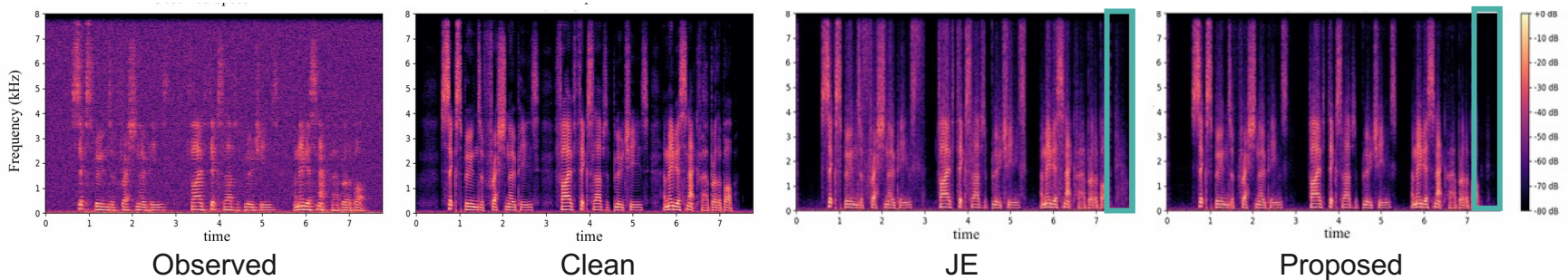
Takeaways
Robust against and positional RIR mismatches, effectively stabilizing the ill-posed system

Application in speech dereverberation

■ Experiments

		$T_{60} \rightarrow$	190 ms				430 ms				890 ms			
SNR (dB)	Error(α) (%)	Methods↓	STOI↑	PESQ↑	F-SNR (dB)↑	Iter.↓	STOI↑	PESQ↑	F-SNR (dB)↑	Iter.↓	STOI↑	PESQ↑	F-SNR (dB)↑	Iter.↓
0 dB	0%	Observed	0.631	1.035	3.772	-	0.548	1.028	3.482	-	0.554	1.048	3.480	-
		JE	0.752	1.074	5.965	81	0.634	1.042	3.400	250	0.728	1.099	6.052	222
		Proposed-s	0.763	1.099	6.318	84	0.648	1.039	3.996	238	0.755	1.156	7.368	270
		Proposed-d	0.821	1.291	9.737	35	0.769	1.190	7.349	38	0.784	1.332	8.782	40
10 dB	0%	Observed	0.718	1.078	5.721	-	0.607	1.034	4.911	-	0.611	1.100	4.496	-
		JE	0.862	1.625	10.636	36	0.801	1.154	7.250	105	0.827	1.698	10.796	124
		Proposed-s	0.868	1.683	11.065	36	0.811	1.208	8.061	112	0.828	1.721	11.869	103
		Proposed-d	0.881	1.868	11.896	36	0.836	1.368	10.116	32	0.848	1.761	11.994	36
20 dB	0%	Observed	0.772	1.313	7.263	-	0.659	1.095	6.205	-	0.635	1.209	5.149	-
		JE-0	0.897	2.104	11.392	9	0.879	1.902	12.321	40	0.873	2.109	13.483	5
		Proposed-s	0.901	2.206	11.430	10	0.888	2.049	12.932	36	0.881	2.482	14.962	24
		Proposed-d	0.900	2.266	11.464	10	0.888	2.118	13.009	36	0.883	2.644	15.489	8
	15%	JE	0.891	2.033	11.050	7	0.882	1.774	11.050	44	0.862	1.887	12.010	43
		Proposed-d	0.896	2.188	11.004	9	0.888	2.068	11.759	36	0.876	2.229	12.455	8

- JE^[1]: Joint enhancement frame work via the PnP strategy to simultaneously execute dereverberation and denoising



Application in speech dereverberation

■ Weighted Prediction Error (WPE) Algorithm -- Multi-channel method

• Multi-channel linear prediction

$$\begin{matrix} & \mathbf{b}_1(n-D, k) \\ \uparrow & \underbrace{} \\ \begin{bmatrix} B_1(n-D, k) & \cdots & B_1(n-D-L, k) \\ \vdots & \ddots & \vdots \\ B_Q(n-D, k) & \cdots & B_Q(n-D-L, k) \end{bmatrix} \end{matrix}$$

- n: Time frame indices
- k: Frequency bin indices
- L: Filter order
- D: Time delay
- Q: Number of channels

• Observed signal:

$$\bar{\mathbf{b}}(n-D, k) = \text{col} \left\{ \underbrace{\mathbf{b}_1(n-D, k), \dots, \mathbf{b}_Q(n-D, k)}_{L \times Q} \right\}$$

- Multi-channel autoregressive model for channel modeling

$$B_{\text{ref}}(n, k) = \hat{S}(n, k) + \bar{\mathbf{w}}^H(k) \bar{\mathbf{b}}(n-D, k)$$

Desired speech Late reverberation part

- Use Gaussian distribution as clean speech prior model, and Maximum likelihood method to construct cost function:

$$\mathcal{J}(\{\bar{\mathbf{w}}(k)\}_{k=1}^K, \{\sigma(k)\}_{k=1}^K) = \sum_{k=1}^K \sum_{n=1}^N \frac{|B_{\text{ref}}(n, k) - \bar{\mathbf{w}}^H(k) \bar{\mathbf{b}}(n-D, k)|^2}{\sigma(n, k)} + \log \pi \sigma(n, k)$$

Alternately estimate

➤ Challenge: Lack data priors → reduces performance under complex conditions

Application in speech dereverberation

■ Current hybrid strategies

- Concatenation $\left\{ \begin{array}{l} \text{Data-driven front-end + physics-based back-} \\ \text{end} \\ \text{Physics-based front-end + data-driven back-end} \end{array} \right.$

- Neural networks estimating intermediate variables in the WPE method
e.g. utilize deep neural network (DNN) to estimate spectrum

$$\mathcal{J}_{\text{WPE}}(\{\overline{\mathbf{w}}(k)\}_{k=1}^K, \{\boldsymbol{\sigma}(k)\}_{k=1}^K) = \sum_{k=1}^K \sum_{n=1}^N \frac{|\hat{S}(n, k)|^2}{\sigma(n, k)} + \log \pi \sigma(n, k)$$



How to integrate the advantages of the two different approaches by formulating the optimization problem from the very beginning?

Application in speech dereverberation

■ Integrating Data Priors to the WPE method

→ Conduct speech dereverberation under **complex conditions**

Complex conditions: Diffuse noise,

Dereverberation + denoise

- The desired speech signal : $R(n, k) = X_{\text{ref}}(n, k) - \bar{\mathbf{w}}^H(k)\bar{\mathbf{x}}(n - D, k) - V(n, k)$
- Insert speech prior via **regularization by denoising (RED)**
- The cost function: $\mathcal{J}_{\text{WPE_Reg}}(\{\bar{\mathbf{w}}(k)\}_{k=1}^K, \{\sigma(k)\}_{k=1}^K) = \mathcal{J}_{\text{WPE}} + \beta \mathcal{J}_{\text{Reg}}(\mathbf{R})$
- The regularization term: $\mathcal{J}_{\text{Reg}}(\mathbf{R}) = \frac{1}{2} \langle \mathbf{R}, \mathbf{R} - \Omega(\mathbf{R}) \rangle$ ← Deep denoiser output
- The **full problem formulation**:

$$\min_{\bar{\mathbf{w}}(k), \sigma(k), \mathbf{R}, \mathbf{V}} \sum_{k=1}^K \sum_{n=1}^N \frac{|\hat{S}(n, k)|^2}{\sigma(n, k)} + \log \pi \sigma(n, k) + \frac{\beta}{2} \langle \mathbf{R}, \mathbf{R} - \Omega(\mathbf{R}) \rangle$$

$$\text{s.t. } R(n, k) = X_{\text{ref}}(n, k) - \bar{\mathbf{w}}^H(k)\bar{\mathbf{x}}(n - D, k) - V(n, k) \text{ for } n = 1, \dots, N \text{ and } k = 1, \dots, K,$$

[1] Z. Yang, W. Yang, K. Xie and J. Chen, “Integrating Data Priors with Weighted Prediction Error for Speech Dereverberation”, IEEE/ACM Transactions on Audio, Speech, Language and Processing, vol. 32, pp. 3908-3923, 2024.

[2] Z. Yang, W. Yang, K. Xie and J. Chen, “Speech Dereverberation Using Weighted Prediction Error with Prior Learnt from Data”, in Proc. EUSIPCO, pp. 356-360, 2023

Application in speech dereverberation

■ Integrating Data Priors to the WPE method

→ Solving method

➤ The corresponding (scaled) **augmented Lagrangian function**

$$\mathcal{L}(\{\bar{\mathbf{w}}(k)\}_{k=1}^K, \{\boldsymbol{\sigma}(k)\}_{k=1}^K, \mathbf{R}, \mathbf{V}, \mathbf{P}) = \mathcal{J}_{\text{WPE}} + \frac{\beta}{2} \langle \mathbf{R}, \mathbf{R} - \Omega(\mathbf{R}) \rangle + \frac{\rho}{2} \sum_{k=1}^K \sum_{n=1}^N \left(|X_{\text{ref}}(n, k) - \bar{\mathbf{w}}^H(k) \times \bar{\mathbf{x}}(n-D, k)] - V(n, k) - R(n, k) + P(n, k)|^2 - |P(n, k)|^2 \right)$$

■ β : Trade-off parameter

■ ρ : Penalty parameter

Scaled dual variable

➤ Using variable splitting method to **solve the problem**

◆ With respect to $\bar{\mathbf{w}}(k)$: $\bar{\mathbf{w}}^{(\ell+1)}(k) = \left[R_{\bar{\mathbf{x}}}^{(\ell+1)}(k) \right]^{-1} \mathbf{P}_{\bar{\mathbf{x}}}^{(\ell+1)}(k)$

◆ With respect to $\boldsymbol{\sigma}(k)$: $\sigma(n, k) = \max \left\{ |\hat{S}(n, k)|^2, \epsilon \right\}$

◆ With respect to $\mathbf{R}$: $\mathbf{R}^{(\ell+1, i+1)} = \left[\mu \tilde{\mathbf{R}}^{(\ell+1)} + (1 - \mu) \Omega \left(\mathbf{R}^{(\ell+1, i)} \right) \right]$ ← *The fixed-point iteration*

◆ With respect to $\mathbf{V}$: $\mathbf{V}^{(\ell+1)} = \hat{\mathbf{S}}^{(\ell+1)} - \mathbf{R}^{(\ell+1)} + \mathbf{P}^{(\ell)}$

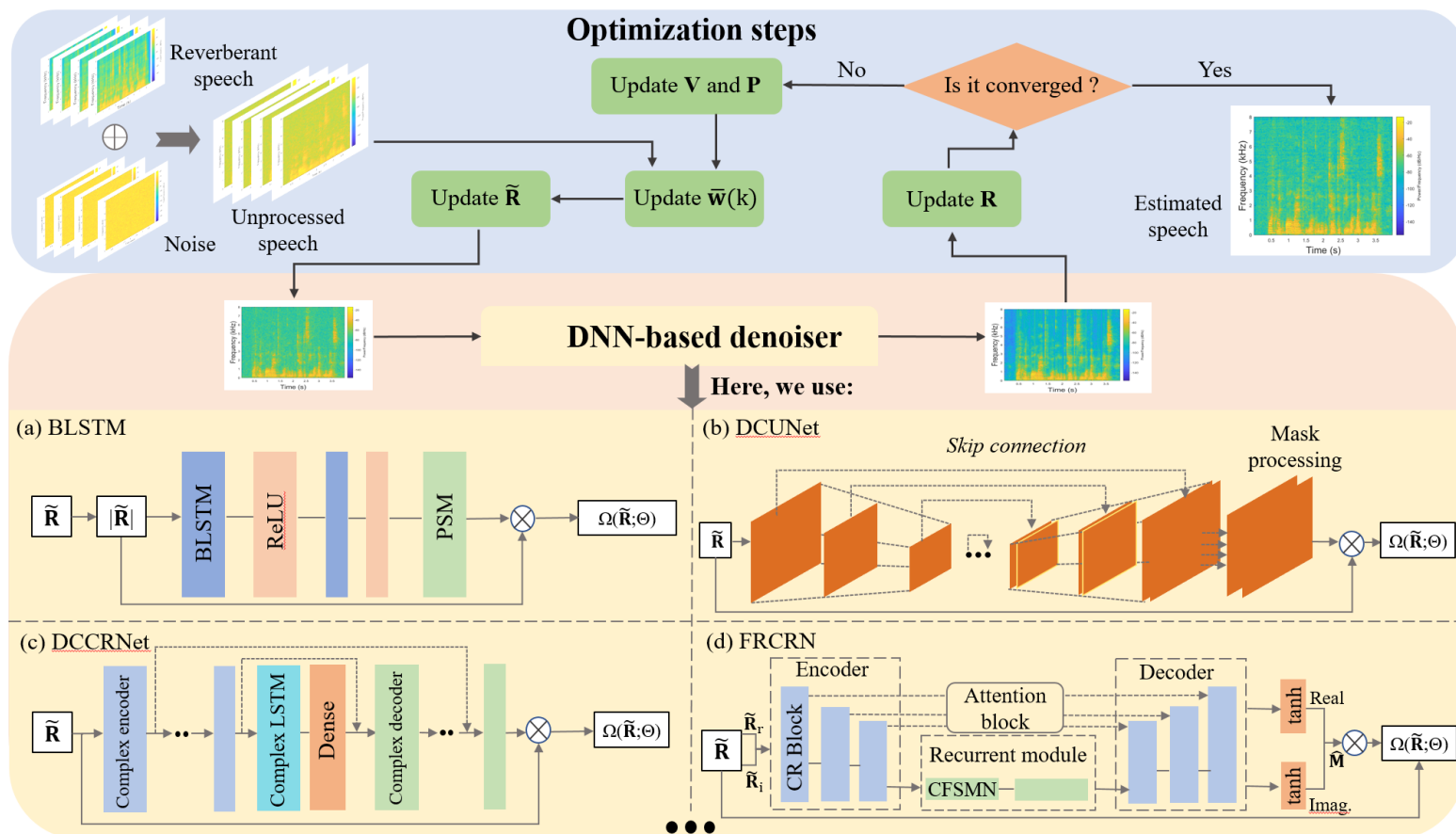
◆ With respect to $\mathbf{P}$: $\mathbf{P}^{(\ell+1)} = \mathbf{P}^{(\ell)} + \hat{\mathbf{S}}^{(\ell+1)} - \mathbf{V}^{(\ell+1)} - \mathbf{R}^{(\ell+1)}$

[1] Z. Yang, W. Yang, K. Xie and J. Chen, "Integrating Data Priors with Weighted Prediction Error for Speech Dereverberation", IEEE/ACM Transactions on Audio, Speech, Language and Processing, vol. 32, pp. 3908-3923, 2024.

[2] Z. Yang, W. Yang, K. Xie and J. Chen, "Speech Dereverberation Using Weighted Prediction Error with Prior Learnt from Data", in Proc. EUSIPCO, pp. 356-360, 2023

Application in speech dereverberation

■ The overall framework



➤ **Takeaway:** The Optimization framework remains the same
The denoiser module is flexible

Application in speech dereverberation

■ Experimental setting

Room type	Room A	Room B
Room length (m)	8-13	15-20
Room width (m)	8-13	15-20
Room height (m)	2.8-3.8	3-4
T60 (ms)	400-800	800-1200
Minimum distance from source to wall (m)	0.5	0.8
Minimum distance from source to microphone (m)	0.8	1.3
Microphone array	Linear array with 4 channels	
	Inner distance = 40 mm	
	Microphone type = Omnidirectional	

Room A

- ◆ Medium room with moderate reverberation

Room B

- ◆ Large room with high reverberation

Corpus:WSJ0

• Evaluation metrics

Perceptual Evaluation of Speech Quality (PESQ) ↑

Short-Time Objective Intelligibility (STOI) ↑

Cepstral Distance(CD) ↓

Frequency-weighted segmental Signal-to-Noise Ratio (F-SNR) ↑

Application in speech dereverberation

■ Experimental results in Room A

Additive noise type	Noise level		SNR = 0 dB			SNR = 10 dB			SNR = 20 dB		
	Method	Denoiser	PESQ	CD	F-SNR	PESQ	CD	F-SNR	PESQ	CD	F-SNR
WGN	Unprocessed	-	1.42	8.47	4.72	1.93	7.97	5.72	2.08	6.69	6.31
	WPE	-	1.31	8.63	4.34	1.87	8.35	5.74	2.28	7.27	7.37
	DNN-WPE	-	1.36	8.49	4.68	1.87	7.75	6.34	2.33	6.67	8.15
	Conv-TasNet	-	1.35	9.04	4.78	1.92	8.26	5.84	2.02	7.18	5.94
	SepFormer	-	1.88	7.14	5.78	2.00	6.95	6.60	2.10	<u>5.60</u>	7.03
	Denoise + WPE	BLSTM	1.56	8.63	4.64	1.96	8.28	5.65	2.54	7.17	7.07
		DCUNet	1.28	8.52	4.67	1.65	8.07	5.74	2.03	6.77	6.56
		DCCRNet	1.17	8.51	4.69	1.93	8.04	5.70	1.91	6.77	6.46
		FRCRN	<u>1.95</u>	8.55	4.56	2.22	8.24	5.69	2.45	7.00	6.48
	WPE + Denoise	BLSTM	1.49	7.94	4.00	1.83	7.36	5.16	2.24	6.44	5.99
		DCUNet	1.47	8.88	4.92	2.06	8.10	6.18	2.59	7.30	6.50
		DCCRNet	1.10	8.68	4.23	1.86	9.36	5.73	2.30	8.33	6.08
		FRCRN	<u>1.94</u>	<u>6.82</u>	<u>5.87</u>	<u>2.26</u>	<u>6.65</u>	<u>6.16</u>	<u>2.65</u>	<u>6.15</u>	<u>6.52</u>
	PnPWPE	BLSTM	1.70	<u>6.79</u>	<u>6.35</u>	<u>2.29</u>	<u>6.81</u>	7.40	<u>2.66</u>	5.33	<u>7.84</u>
		DCUNet	1.41	8.44	5.12	2.18	7.71	6.75	2.64	6.24	7.68
		DCCRNet	1.20	8.89	4.79	2.03	8.36	6.47	2.54	6.66	7.65
		FRCRN	1.97	6.34	6.38	2.44	5.69	<u>7.15</u>	2.67	5.33	<u>7.84</u>
Cafe	Unprocessed	-	1.31	6.92	3.04	2.04	6.19	4.60	2.08	5.47	6.07
	WPE	-	1.63	7.05	2.93	2.03	6.19	4.69	2.32	4.75	6.73
	DNN-WPE	-	1.66	6.54	4.77	2.29	5.68	6.67	2.37	4.55	7.77
	Conv-TasNet	-	1.53	6.91	4.54	1.98	6.14	5.56	2.23	5.43	6.50
	SepFormer	-	1.73	6.54	4.87	2.11	5.82	5.78	2.09	5.15	6.93
	Denoise + WPE	BLSTM	1.04	6.87	2.85	1.71	6.25	4.35	2.33	5.19	6.14
		DCUNet	1.35	6.94	2.98	2.02	6.21	4.47	2.14	5.27	6.10
		DCCRNet	1.32	6.92	3.02	1.87	6.21	4.44	2.00	5.39	6.01
		FRCRN	1.70	7.03	3.10	2.06	6.32	4.55	2.33	5.52	6.10
	WPE + Denoise	BLSTM	0.97	8.20	3.29	1.69	7.17	5.04	2.32	5.14	6.83
		DCUNet	1.67	7.82	4.11	2.13	7.31	5.48	2.48	6.24	7.23
		DCCRNet	1.58	8.49	4.89	1.67	7.20	5.92	2.31	7.26	6.79
		FRCRN	<u>1.70</u>	<u>6.44</u>	<u>4.82</u>	<u>2.20</u>	<u>5.91</u>	<u>6.00</u>	2.58	<u>4.72</u>	<u>7.46</u>
	PnPWPE	BLSTM	1.54	6.79	3.62	2.24	5.83	5.62	2.45	4.54	7.32
		DCUNet	1.58	6.71	4.05	<u>2.33</u>	<u>5.63</u>	5.78	<u>2.55</u>	<u>4.45</u>	7.21
		DCCRNet	<u>1.82</u>	6.85	4.79	2.25	5.52	<u>6.15</u>	2.48	4.50	7.25
		FRCRN	1.88	6.34	4.41	2.34	5.52	5.73	2.58	4.33	7.34

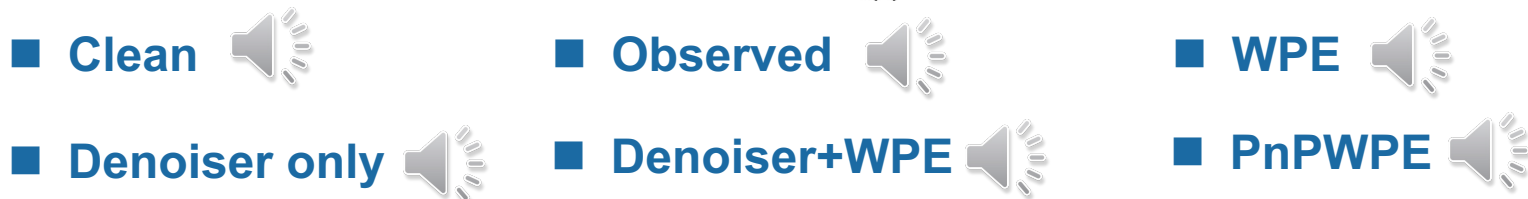
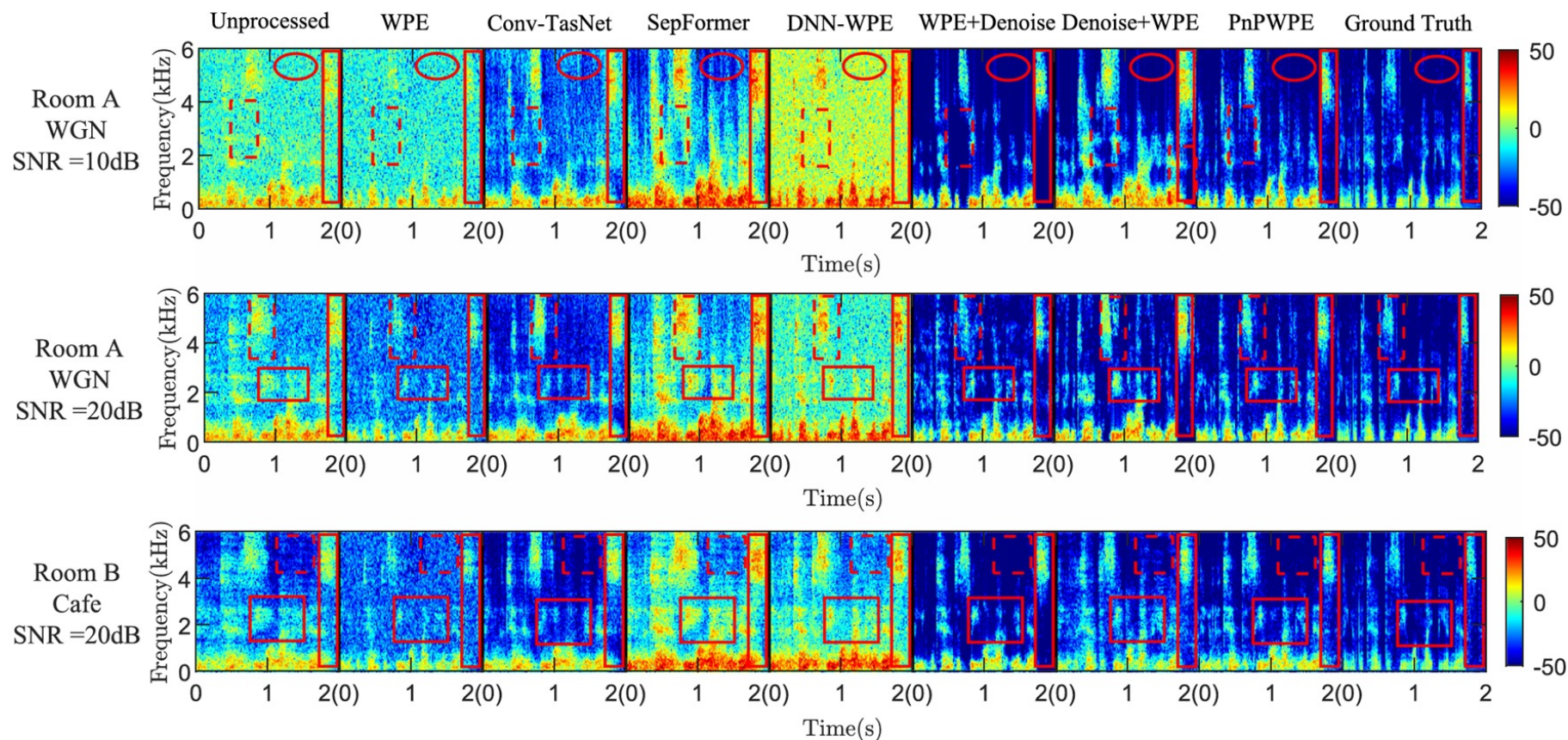
Application in speech dereverberation

■ Experimental results in Room B

Additive noise type	Noise level		SNR = 0 dB			SNR = 10 dB			SNR = 20 dB		
	Method	Denoiser	PESQ	CD	F-SNR	PESQ	CD	F-SNR	PESQ	CD	F-SNR
WGN	Unprocessed	-	1.21	8.42	4.61	1.48	7.94	5.61	1.71	6.75	6.09
	WPE	-	1.22	8.59	4.32	1.69	8.29	5.73	2.14	7.24	7.37
	DNN-WPE	-	1.75	8.66	4.39	1.74	7.78	5.97	2.14	6.32	8.53
	Conv-TasNet	-	0.67	9.11	4.38	1.64	8.26	5.70	1.81	7.29	5.70
	SepFormer	-	1.77	7.19	5.06	1.96	7.07	5.99	1.98	6.18	6.57
	Denoise + WPE	BLSTM	1.47	8.70	4.57	1.77	8.32	5.50	2.21	7.24	6.97
		DCUNet	0.94	8.48	4.57	1.50	8.05	5.52	1.61	6.78	6.25
		DCCRNNet	0.75	8.47	4.59	1.23	8.02	5.53	1.44	6.82	6.09
		FRCRN	1.77	8.51	4.47	1.42	8.15	5.45	2.17	7.13	5.79
	WPE + Denoise	BLSTM	1.46	8.00	3.68	1.61	7.47	4.98	1.98	6.51	5.98
		DCUNet	1.16	8.89	4.57	1.81	8.15	6.11	2.24	7.54	6.45
		DCCRNNet	0.71	9.68	3.93	1.55	9.41	5.48	2.21	8.39	6.05
		FRCRN	1.78	6.92	5.46	2.01	6.66	5.97	2.39	6.11	6.57
	PnPWPE	BLSTM	1.58	7.02	5.99	1.98	6.38	7.02	2.28	5.36	7.84
		DCUNet	1.22	8.38	4.95	1.85	7.74	6.51	2.37	6.43	7.76
		DCCRNNet	1.19	8.69	4.56	1.82	8.23	6.13	2.40	6.73	7.81
		FRCRN	1.82	6.37	5.96	2.08	6.45	7.11	2.33	5.17	7.58
Cafe	Unprocessed	-	1.33	6.88	3.49	1.57	6.30	4.46	1.67	5.76	5.46
	WPE	-	1.38	7.06	3.26	1.89	6.17	4.50	2.09	4.99	6.01
	DNN-WPE	-	1.40	6.97	4.52	1.95	5.77	5.07	2.14	4.42	6.07
	Conv-TasNet	-	1.19	6.78	4.96	1.81	6.32	5.41	1.87	5.76	5.79
	SepFormer	-	1.42	6.73	5.30	1.76	5.70	5.44	1.86	5.62	6.43
	Denoise + WPE	BLSTM	0.96	6.85	3.44	1.57	6.42	4.04	1.86	5.53	6.39
		DCUNet	0.94	6.85	3.41	1.68	6.31	4.30	1.70	5.54	5.45
		DCCRNNet	0.75	6.87	3.39	1.58	6.29	4.23	1.65	5.70	5.27
		FRCRN	1.47	7.01	3.49	2.03	6.56	4.29	2.14	5.86	5.37
	WPE + Denoise	BLSTM	0.47	8.24	3.20	1.62	7.28	4.80	1.95	5.53	6.39
		DCUNet	1.17	7.80	4.28	1.74	7.18	5.38	2.06	6.76	6.42
		DCCRNNet	1.03	8.51	4.89	1.67	7.69	5.30	1.99	7.34	6.08
		FRCRN	1.14	6.52	4.83	1.98	5.99	5.65	2.16	5.23	6.63
	PnPWPE	BLSTM	1.37	6.82	3.82	2.08	7.28	4.80	2.11	4.88	6.37
		DCUNet	1.42	6.79	3.94	2.00	5.74	5.38	2.14	4.88	6.35
		DCCRNNet	1.50	6.64	4.50	2.03	5.60	5.69	2.13	4.85	6.41
		FRCRN	1.41	6.48	4.23	2.08	5.66	5.62	2.26	4.79	6.52

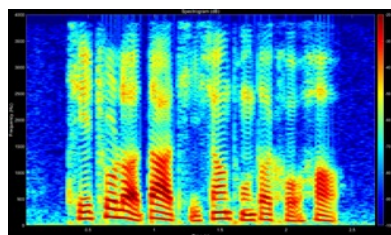
Application in speech dereverberation

■ Visualization results

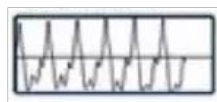


Application in speech separation

- Speech separation is to separate multiple speakers and reduce mutual interference.

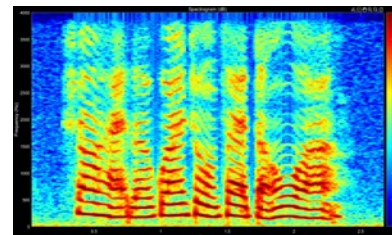
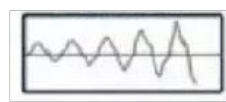


Speaker 1

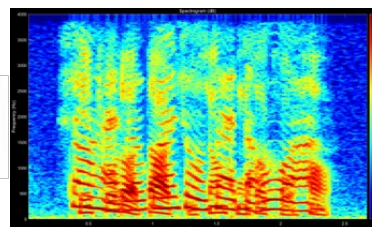
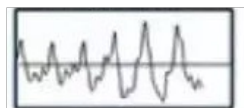


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Speaker 2

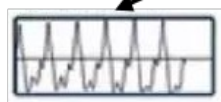
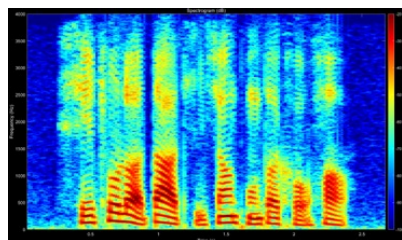


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Mixture

Speech Separation

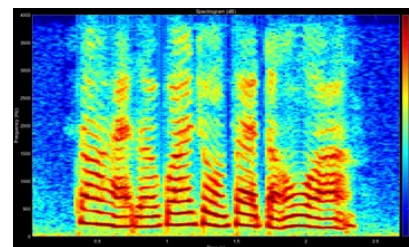


Speaker 1

Predicted



Speaker 2

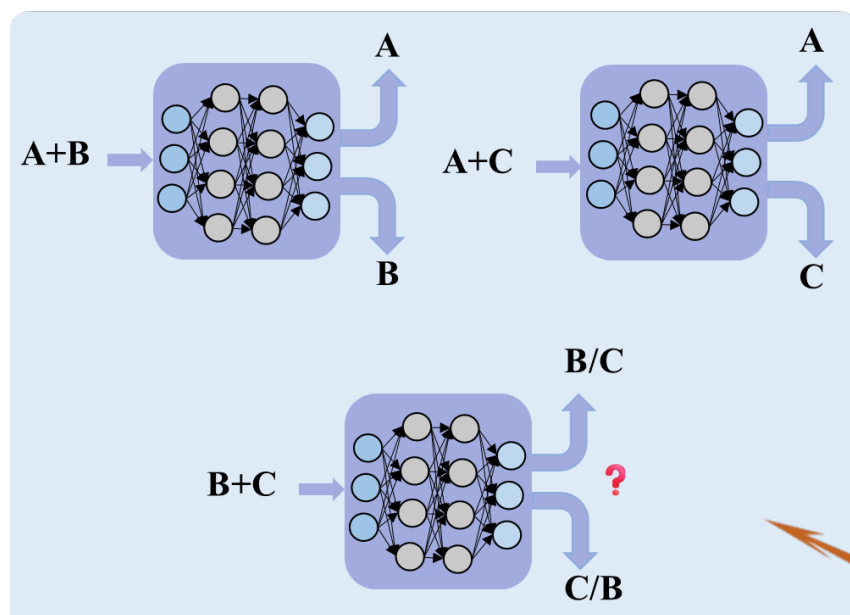


Application in speech separation

■ Current data-driven methods

➤ Time-Frequency domain

Learn speech characteristics in time-frequency space



The optimization objective is ill-defined, causing gradient reversal and leading to training failure. ✖

- ✓ Deep clustering
- ✓ Permutation invariant training (PIT)

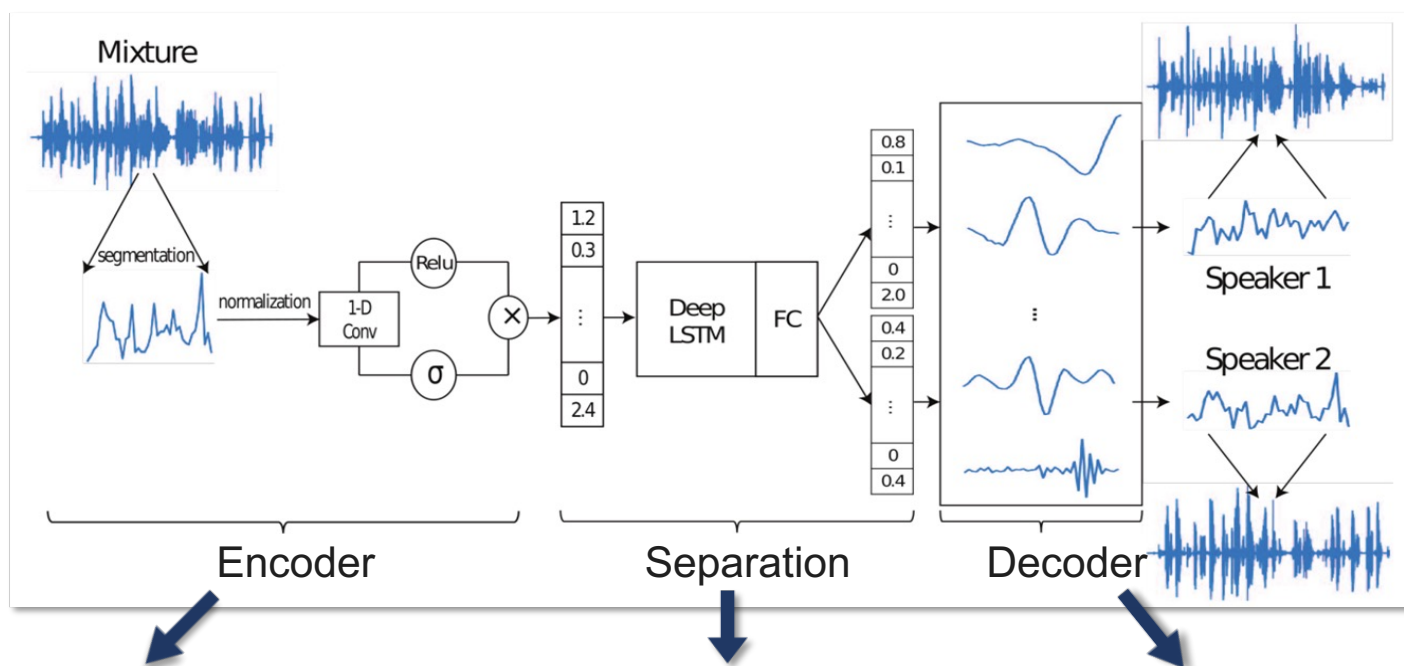
Two perspectives to address the speaker permutation problem

Application in speech separation

■ Current data-driven methods

➤ Time domain

waveform-level modeling



Convert mixture waveform into latent representation

Conv-TasNet -- Temporal convolutional networks
DPRNN -- Dual-path RNN for long sequences
SepFormer -- Transformer-based separation

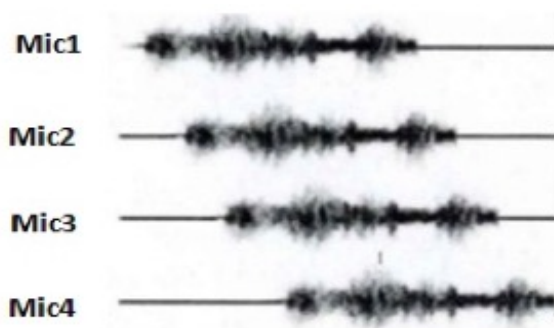
Reconstruct separated waveforms back to time domain

Application in speech separation

■ Current traditional methods

◆ Spatial filtering -- Beamforming

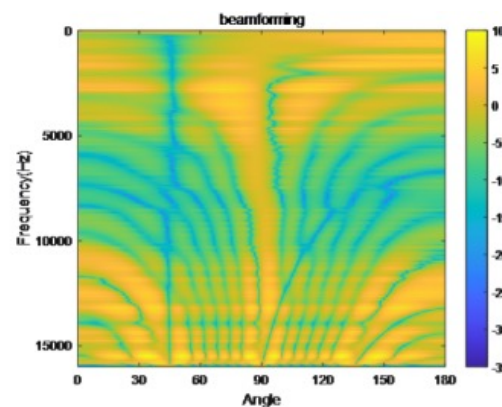
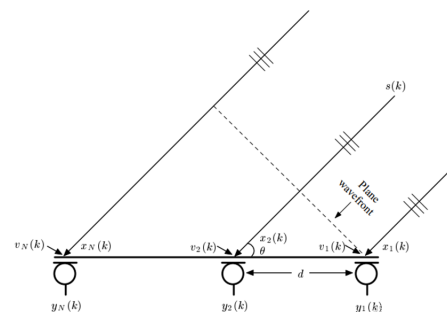
➤ Delay and Sum beamforming



$$\text{Output} = \sum_i (Mic_i(t + i\tau))$$

- Accurate estimation of time-of-arrival is challenging in reverberant environments.
- Not robust against diffuse noise

➤ Adaptive beamforming



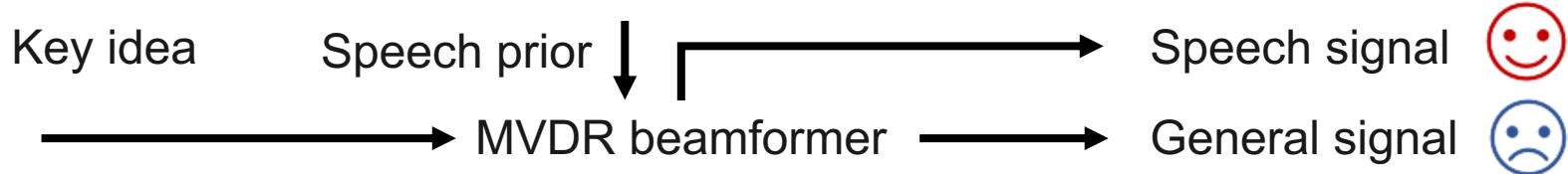
Minimum Variance Distortionless Response (MVDR) beamforming

$$\begin{aligned} \omega^* &= \arg \min_{\omega} \omega^H R_x \omega \\ \text{s.t. } \omega^H a(\theta_d) &= 1 \end{aligned}$$

- The direction of the interference is known.

Application in speech separation

■ Hybrid strategy -- PnPMVDR



- The corresponding (scaled) **augmented Lagrangian function**

$$\mathcal{L}(\mathbf{w}(k), \mathbf{R}, \mathbf{V}, \mathbf{P}) = \frac{1}{N} \sum_{k=1}^K \|\mathbf{w}^H(k) \mathbf{X}(k)\|_2^2 + \frac{\beta}{2} \langle \mathbf{R}, \mathbf{R} - \Omega(\mathbf{R}) \rangle \text{ regularization} \\ + \frac{\rho}{2} \sum_{k=1}^K \left(\|\mathbf{w}^H(k) \mathbf{X}(k) - \mathbf{R}(k) - \mathbf{V}(k) + \mathbf{P}(k)\|_2^2 \right) - \frac{\rho}{2} \sum_{k=1}^K (\|\mathbf{P}(k)\|_2^2) + \sum_{k=1}^K \lambda(k) (\mathbf{w}^H(k) \mathbf{a}(k) - 1)$$

■ β : Trade-off parameter ■ ρ : Penalty parameter

- Using variable splitting method to **solving the problem**

- ◆ With respect to $\bar{\mathbf{w}}(k)$: $\mathbf{w}^{(\ell+1)}(k) = \frac{1}{N\rho + 2} \mathbf{R}_x^{-1}(k) \left\{ \rho [\mathbf{Z}^{(\ell)}(k)]^H - \mathbf{F}^{(\ell)}(k) \right\}$
- ◆ With respect to $\mathbf{R}$: $\mathbf{R}^{(\ell+1, i+1)} = \mu \tilde{\mathbf{R}}^{(\ell+1)} + (1 - \mu) \Omega(\mathbf{R}^{(\ell+1, i)})$ ← The fixed-point iteration with the denoiser prior
- ◆ With respect to $\mathbf{P}$: $\mathbf{P}^{(\ell+1)} = \mathbf{P}^{(\ell)} + \hat{\mathbf{S}}^{(\ell+1)} - \mathbf{R}^{(\ell+1)} - \mathbf{V}^{(\ell)}$
- ◆ With respect to $\mathbf{V}$: $\mathbf{V}^{(\ell+1)} = \hat{\mathbf{S}}^{(\ell+1)} - \mathbf{R}^{(\ell+1)} + \mathbf{P}^{(\ell+1)}$

Application in speech separation

- Deep denoiser: Frequency Recurrent Convolutional Recurrent Networks^[1]
- additive noise: WGN

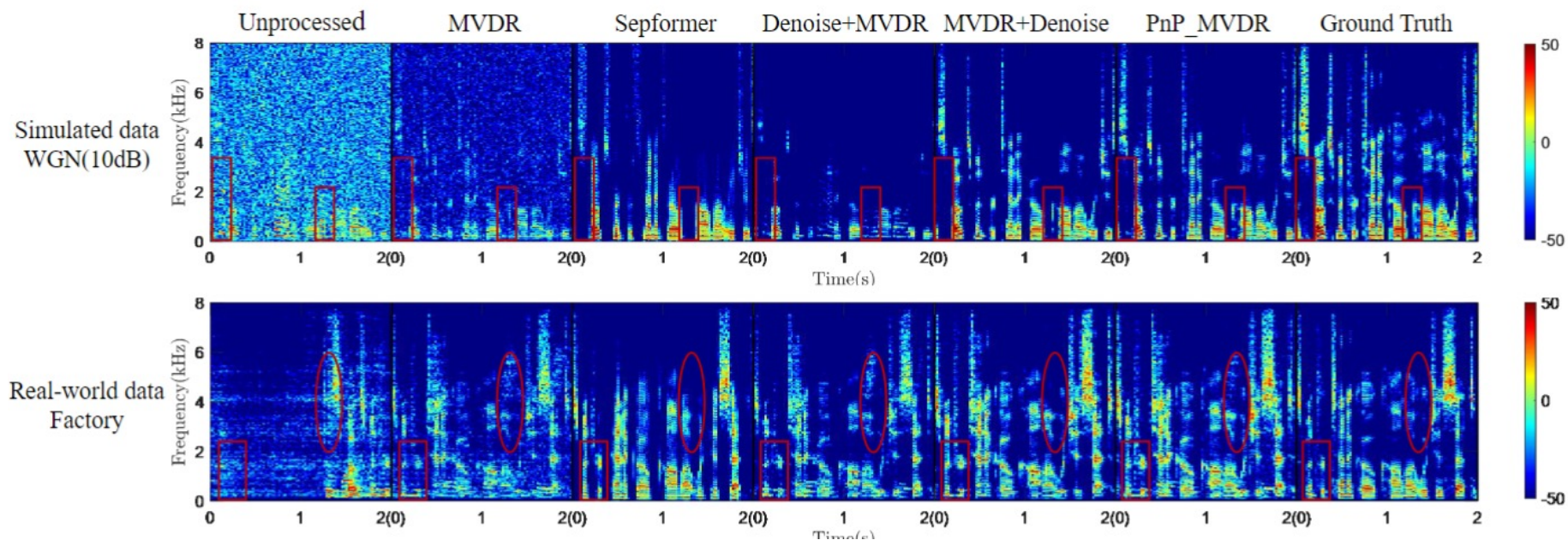
Noise level	Comparison methods	Speaker 1			Speaker 2		
		fwSNRseg (dB) ↑	PESQ ↑	STOI ↑	fwSNRseg (dB) ↑	PESQ ↑	STOI ↑
SNR = 10 dB	Unprocessed speech	5.59	1.19	0.59	6.73	1.84	0.84
	MVDR	9.62	2.17	0.94	9.22	2.33	0.94
	FRCRN+MVDR	7.06	1.95	0.81	7.21	2.13	0.89
	MVDR+FRCRN	12.17	3.23	0.98	11.80	3.23	0.96
	Proposed	13.28	3.29	0.98	12.42	3.26	0.96
		$(\rho = 95, \mu = 0.40)$			$(\rho = 95, \mu = 0.25)$		
SNR = 0 dB	Unprocessed speech	4.61	0.98	0.50	5.27	1.45	0.75
	MVDR	6.51	1.49	0.78	7.21	1.94	0.89
	FRCRN+MVDR	4.58	1.62	0.66	6.28	2.17	0.87
	MVDR+FRCRN	9.60	2.69	0.94	9.89	2.73	0.95
	Proposed	10.92	2.77	0.94	11.23	2.81	0.95
		$(\rho = 80, \mu = 0.45)$			$(\rho = 5, \mu = 0.45)$		
SNR = -10 dB	Unprocessed speech	4.41	0.96	0.41	4.65	1.00	0.56
	MVDR	4.88	0.98	0.53	5.28	1.39	0.75
	FRCRN+MVDR	2.97	1.09	0.38	3.90	1.91	0.77
	MVDR+FRCRN	4.34	1.24	0.61	7.92	2.27	0.89
	Proposed	6.25	1.30	0.61	9.12	2.37	0.89
		$(\rho = 95, \mu = 0.50)$			$(\rho = 50, \mu = 0.35)$		

Takeaway: By plugging speech priors into the MVDR framework, we can significantly enhance both speech quality and intelligibility under noisy environments

[1] S. Zhao, B. Ma, K.N. Watcharasupat, and W.-S. Gan, "FRCRN: Boosting feature representation using frequency recurrence for monaural speech enhancement," in Proc. 2022 IEEE Int. Conf. Acoust., Speech, Signal Process., May 2022, pp. 9281–9285.

Application in speech separation

■ PnPMVDR



■ Clean 

■ Observed 

■ MVDR + Denoise 

■ PnPMVDR 

Outline

Introduction

Part I: Methodology

- General Problem Formulation

- Hybrid Approaches for Parameter Estimation

- State-of-the-Art Hybrid Techniques

Part II: Applications to Image Processing

- Background in Hyperspectral Imaging

- Hybrid Strategies for Hyperspectral Deconvolution

- Hybrid Strategies for Hyperspectral Fusion

- Hybrid Strategies for Hyperspectral Unmixing

Part III: Applications to Speech Signal Processing

- Background in Speech Processing

- Hybrid Strategies for Speech Dereverberation

- Hybrid Strategies for Speech Separation

Future Directions

Future Directions

1.

Extend hybrid methodologies to new modalities

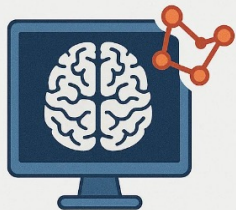
2.

Bridging the theory–practice gap

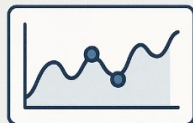
3.

Leveraging large language models

HYBRID METHODOLOGIES

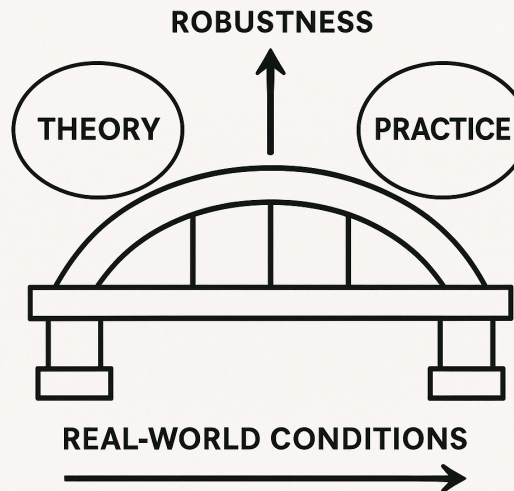


MEDICAL IMAGING

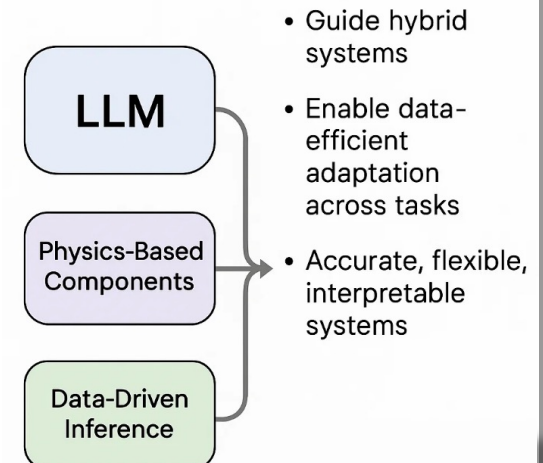


MULTIMODAL
SPEECH PROCESSING

Bridging the Theory–Practice Gap to Ensure Robustness Under Real-World Conditions



Leveraging Large Language Models (LLMs)





Thanks!

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Northwestern Polytechnical University, China.**

[†]Université de Lorraine, CRAN, CNRS, France.